

Edexcel Maths M1

Past Paper Pack

2005-2013

Centre No.						Paper Reference						Surname	Initial(s)	
Candidate No.						6	6	7	7	/	0	1	Signature	

Paper Reference(s)

6677/01

Edexcel GCE

Mechanics M1

Advanced/Advanced Subsidiary

Wednesday 12 January 2005 – Afternoon

Time: 1 hour 30 minutes

Examiner's use only

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Team Leader's use only

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Question Number	Leave Blank
1	
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Total	

Materials required for examination Items included with question papers
 Mathematical Formulae (Lilac or Green) Nil

Candidates may use any calculator EXCEPT those with facility for symbolic algebra, differentiation and/or integration. Thus candidates may NOT use calculators such as the Texas Instruments T1 89, T1 92, Casio CFX 9970G, Hewlett Packard HP 48G.

Instructions to Candidates

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Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided. Full marks may be obtained for answers to ALL questions. This paper has seven questions. There are no blank pages. The total mark for this paper is 75.

Advice to Candidates

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1. A particle P of mass 1.5 kg is moving along a straight horizontal line with speed 3 m s^{-1} . Another particle Q of mass 2.5 kg is moving, in the opposite direction, along the same straight line with speed 4 m s^{-1} . The particles collide. Immediately after the collision the direction of motion of P is reversed and its speed is 2.5 m s^{-1} .

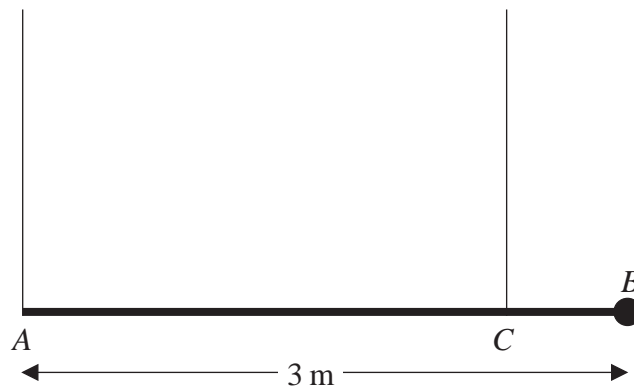
(a) Calculate the speed of Q immediately after the impact. (3)

(b) State whether or not the direction of motion of Q is changed by the collision. (1)

(c) Calculate the magnitude of the impulse exerted by Q on P , giving the units of your answer. (3)

2.

Figure 1



A plank AB has mass 40 kg and length 3 m . A load of mass 20 kg is attached to the plank at B . The loaded plank is held in equilibrium, with AB horizontal, by two vertical ropes attached at A and C , as shown in Figure 1. The plank is modelled as a uniform rod and the load as a particle. Given that the tension in the rope at C is three times the tension in the rope at A , calculate

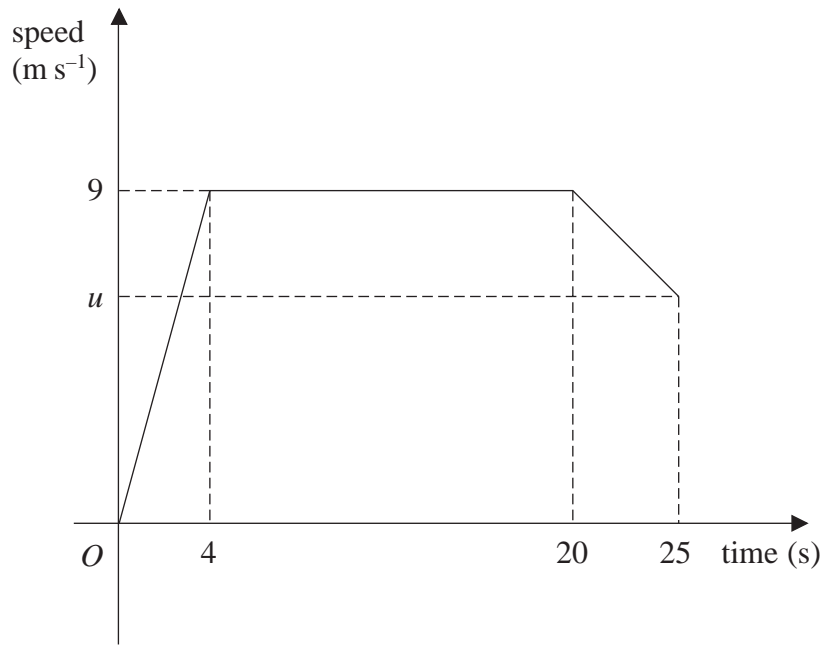
(a) the tension in the rope at C , (2)

(b) the distance CB . (5)

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3.

Figure 2



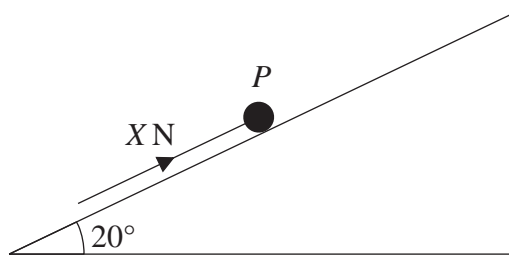
A sprinter runs a race of 200 m. Her total time for running the race is 25 s. Figure 2 is a sketch of the speed-time graph for the motion of the sprinter. She starts from rest and accelerates uniformly to a speed of 9 m s^{-1} in 4 s. The speed of 9 m s^{-1} is maintained for 16 s and she then decelerates uniformly to a speed of $u \text{ m s}^{-1}$ at the end of the race. Calculate

- (a) the distance covered by the sprinter in the first 20 s of the race, (2)
- (b) the value of u , (4)
- (c) the deceleration of the sprinter in the last 5 s of the race. (3)

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4.

Figure 3



A particle P of mass 2.5 kg rests in equilibrium on a rough plane under the action of a force of magnitude X newtons acting up a line of greatest slope of the plane, as shown in Figure 3. The plane is inclined at 20° to the horizontal. The coefficient of friction between P and the plane is 0.4 . The particle is in limiting equilibrium and is on the point of moving up the plane. Calculate

- (a) the normal reaction of the plane on P , (2)

- (b) the value of X . (4)

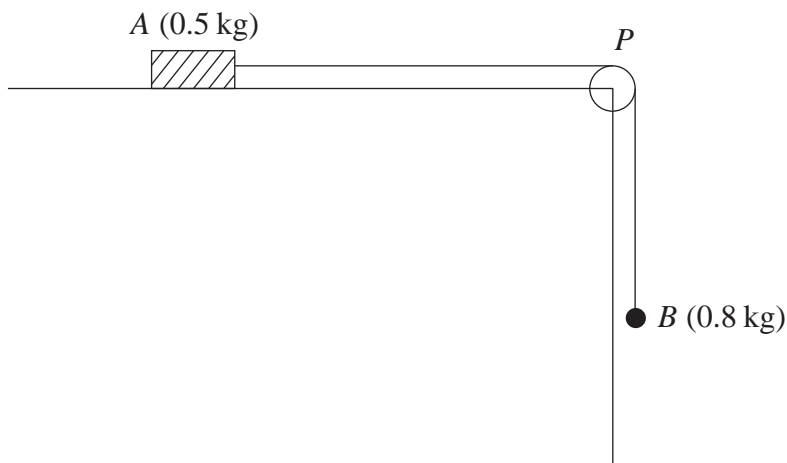
The force of magnitude X newtons is now removed.

- (c) Show that P remains in equilibrium on the plane. (4)

Leave blank

5.

Figure 4



A block of wood A of mass 0.5 kg rests on a rough horizontal table and is attached to one end of a light inextensible string. The string passes over a small smooth pulley P fixed at the edge of the table. The other end of the string is attached to a ball B of mass 0.8 kg which hangs freely below the pulley, as shown in Figure 4. The coefficient of friction between A and the table is μ . The system is released from rest with the string taut. After release, B descends a distance of 0.4 m in 0.5 s . Modelling A and B as particles, calculate

- (a) the acceleration of B , (3)
- (b) the tension in the string, (4)
- (c) the value of μ . (5)
- (d) State how in your calculations you have used the information that the string is inextensible. (1)

Leave blank

6. A stone S is sliding on ice. The stone is moving along a straight horizontal line ABC , where $AB = 24$ m and $AC = 30$ m. The stone is subject to a constant resistance to motion of magnitude 0.3 N. At A the speed of S is 20 m s⁻¹, and at B the speed of S is 16 m s⁻¹. Calculate

(a) the deceleration of S , (2)

(b) the speed of S at C . (3)

(c) Show that the mass of S is 0.1 kg. (2)

At C , the stone S hits a vertical wall, rebounds from the wall and then slides back along the line CA . The magnitude of the impulse of the wall on S is 2.4 Ns and the stone continues to move against a constant resistance of 0.3 N.

(d) Calculate the time between the instant that S rebounds from the wall and the instant that S comes to rest. (6)

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7. Two ships P and Q are travelling at night with constant velocities. At midnight, P is at the point with position vector $(20\mathbf{i} + 10\mathbf{j})$ km relative to a fixed origin O . At the same time, Q is at the point with position vector $(14\mathbf{i} - 6\mathbf{j})$ km. Three hours later, P is at the point with position vector $(29\mathbf{i} + 34\mathbf{j})$ km. The ship Q travels with velocity $12\mathbf{j}$ km h⁻¹. At time t hours after midnight, the position vectors of P and Q are \mathbf{p} km and \mathbf{q} km respectively. Find

(a) the velocity of P , in terms of \mathbf{i} and \mathbf{j} , (2)

(b) expressions for \mathbf{p} and \mathbf{q} , in terms of t , \mathbf{i} and \mathbf{j} . (4)

At time t hours after midnight, the distance between P and Q is d km.

(c) By finding an expression for \overrightarrow{PQ} , show that

$$d^2 = 25t^2 - 92t + 292. \tag{5}$$

Weather conditions are such that an observer on P can only see the lights on Q when the distance between P and Q is 15 km or less. Given that when $t = 1$, the lights on Q move into sight of the observer,

(d) find the time, to the nearest minute, at which the lights on Q move out of sight of the observer. (5)

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Paper Reference(s)

6677/01

Edexcel GCE

Mechanics M1

Advanced/Advanced Subsidiary

Tuesday 7 June 2005 – Afternoon

Time: 1 hour 30 minutes

Materials required for examination **Items included with question papers**
Mathematical Formulae (Lilac or Green) Nil

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Examiner's use only

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Team Leader's use only

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Question Number	Leave Blank
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Information for Candidates

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Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 8 questions in this question paper. The total mark for this paper is 75.

There are 20 pages in this question paper. Any blank pages are indicated.

Advice to Candidates

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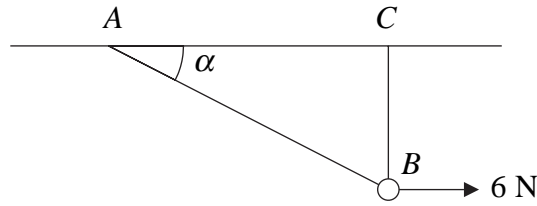
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3.

Figure 1



A smooth bead B is threaded on a light inextensible string. The ends of the string are attached to two fixed points A and C on the same horizontal level. The bead is held in equilibrium by a horizontal force of magnitude 6 N acting parallel to AC . The bead B is vertically below C and $\angle BAC = \alpha$, as shown in Figure 1. Given that $\tan \alpha = \frac{3}{4}$, find

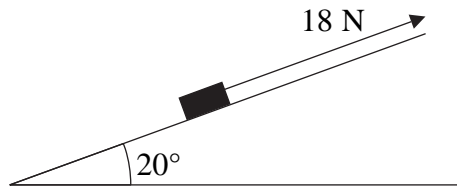
- (a) the tension in the string, (3)
- (b) the weight of the bead. (4)



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4.

Figure 2



A box of mass 2 kg is pulled up a rough plane face by means of a light rope. The plane is inclined at an angle of 20° to the horizontal, as shown in Figure 2. The rope is parallel to a line of greatest slope of the plane. The tension in the rope is 18 N . The coefficient of friction between the box and the plane is 0.6 . By modelling the box as a particle, find

(a) the normal reaction of the plane on the box, (3)

(b) the acceleration of the box. (5)



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5. A train is travelling at 10 m s^{-1} on a straight horizontal track. The driver sees a red signal 135 m ahead and immediately applies the brakes. The train immediately decelerates with constant deceleration for 12 s, reducing its speed to 3 m s^{-1} . The driver then releases the brakes and allows the train to travel at a constant speed of 3 m s^{-1} for a further 15 s. He then applies the brakes again and the train slows down with constant deceleration, coming to rest as it reaches the signal.

(a) Sketch a speed-time graph to show the motion of the train, (3)

(b) Find the distance travelled by the train from the moment when the brakes are first applied to the moment when its speed first reaches 3 m s^{-1} . (2)

(c) Find the total time from the moment when the brakes are first applied to the moment when the train comes to rest. (5)



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Question 5 continued

Lined area for student response, consisting of approximately 25 horizontal lines.

Q5

(Total 10 marks)

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7.

Figure 4

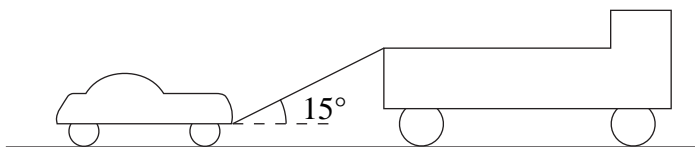


Figure 4 shows a lorry of mass 1600 kg towing a car of mass 900 kg along a straight horizontal road. The two vehicles are joined by a light towbar which is at an angle of 15° to the road. The lorry and the car experience constant resistances to motion of magnitude 600 N and 300 N respectively. The lorry's engine produces a constant horizontal force on the lorry of magnitude 1500 N. Find

(a) the acceleration of the lorry and the car, (3)

(b) the tension in the towbar. (4)

When the speed of the vehicles is 6 m s^{-1} , the towbar breaks. Assuming that the resistance to the motion of the car remains of constant magnitude 300 N,

(c) find the distance moved by the car from the moment the towbar breaks to the moment when the car comes to rest. (4)

(d) State whether, when the towbar breaks, the normal reaction of the road on the car is increased, decreased or remains constant. Give a reason for your answer. (2)



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Question 7 continued

A series of horizontal lines for writing the answer to Question 7.



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8. [In this question, the unit vectors \mathbf{i} and \mathbf{j} are horizontal vectors due east and north respectively.]

At time $t = 0$, a football player kicks a ball from the point A with position vector $(2\mathbf{i} + \mathbf{j})$ m on a horizontal football field. The motion of the ball is modelled as that of a particle moving horizontally with constant velocity $(5\mathbf{i} + 8\mathbf{j})$ m s⁻¹. Find

- (a) the speed of the ball, (2)

- (b) the position vector of the ball after t seconds. (2)

The point B on the field has position vector $(10\mathbf{i} + 7\mathbf{j})$ m.

- (c) Find the time when the ball is due north of B . (2)

At time $t = 0$, another player starts running due north from B and moves with constant speed v m s⁻¹. Given that he intercepts the ball,

- (d) find the value of v . (6)

- (e) State one physical factor, other than air resistance, which would be needed in a refinement of the model of the ball's motion to make the model more realistic. (1)



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Question 8 continued

Ruled area for writing answers.

Q8

(Total 13 marks)

TOTAL FOR PAPER: 75 MARKS

END



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2. (a) Two particles *A* and *B*, of mass 3 kg and 2 kg respectively, are moving in the same direction on a smooth horizontal table when they collide directly. Immediately before the collision, the speed of *A* is 4 m s^{-1} and the speed of *B* is 1.5 m s^{-1} . In the collision, the particles join to form a single particle *C*.

Find the speed of *C* immediately after the collision.

(3)

- (b) Two particles *P* and *Q* have mass 3 kg and m kg respectively. They are moving towards each other in opposite directions on a smooth horizontal table. Each particle has speed 4 m s^{-1} , when they collide directly. In this collision, the direction of motion of each particle is reversed. The speed of *P* immediately after the collision is 2 m s^{-1} and the speed of *Q* is 1 m s^{-1} . Find

- (i) the value of m ,

(3)

- (ii) the magnitude of the impulse exerted on *Q* in the collision.

(2)



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Question 2 continued

Lined area for writing the answer to Question 2.

(Total 8 marks)

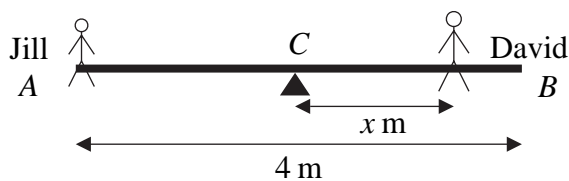
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3.

Figure 1



A seesaw in a playground consists of a beam AB of length 4 m which is supported by a smooth pivot at its centre C . Jill has mass 25 kg and sits on the end A . David has mass 40 kg and sits at a distance x metres from C , as shown in Figure 1. The beam is initially modelled as a uniform rod. Using this model,

(a) find the value of x for which the seesaw can rest in equilibrium in a horizontal position. (3)

(b) State what is implied by the modelling assumption that the beam is uniform. (1)

David realises that the beam is not uniform as he finds that he must sit at a distance 1.4 m from C for the seesaw to rest horizontally in equilibrium. The beam is now modelled as a non-uniform rod of mass 15 kg. Using this model,

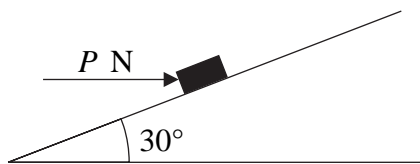
(c) find the distance of the centre of mass of the beam from C . (4)



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5.

Figure 2



A parcel of weight 10 N lies on a rough plane inclined at an angle of 30° to the horizontal. A horizontal force of magnitude P newtons acts on the parcel, as shown in Figure 2. The parcel is in equilibrium and on the point of slipping up the plane. The normal reaction of the plane on the parcel is 18 N. The coefficient of friction between the parcel and the plane is μ . Find

(a) the value of P , (4)

(b) the value of μ . (5)

The horizontal force is removed.

(c) Determine whether or not the parcel moves. (5)



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6. [In this question the horizontal unit vectors \mathbf{i} and \mathbf{j} are due east and due north respectively.]

A model boat A moves on a lake with constant velocity $(-\mathbf{i} + 6\mathbf{j}) \text{ m s}^{-1}$. At time $t = 0$, A is at the point with position vector $(2\mathbf{i} - 10\mathbf{j}) \text{ m}$. Find

(a) the speed of A , (2)

(b) the direction in which A is moving, giving your answer as a bearing. (3)

At time $t = 0$, a second boat B is at the point with position vector $(-26\mathbf{i} + 4\mathbf{j}) \text{ m}$.

Given that the velocity of B is $(3\mathbf{i} + 4\mathbf{j}) \text{ m s}^{-1}$,

(c) show that A and B will collide at a point P and find the position vector of P . (5)

Given instead that B has speed 8 m s^{-1} and moves in the direction of the vector $(3\mathbf{i} + 4\mathbf{j})$,

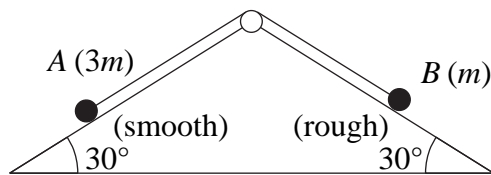
(d) find the distance of B from P when $t = 7 \text{ s}$. (6)



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7.

Figure 3



A fixed wedge has two plane faces, each inclined at 30° to the horizontal. Two particles A and B , of mass $3m$ and m respectively, are attached to the ends of a light inextensible string. Each particle moves on one of the plane faces of the wedge. The string passes over a small smooth light pulley fixed at the top of the wedge. The face on which A moves is smooth. The face on which B moves is rough. The coefficient of friction between B and this face is μ . Particle A is held at rest with the string taut. The string lies in the same vertical plane as lines of greatest slope on each plane face of the wedge, as shown in Figure 3.

The particles are released from rest and start to move. Particle A moves downwards and B moves upwards. The accelerations of A and B each have magnitude $\frac{1}{10}g$.

- (a) By considering the motion of A , find, in terms of m and g , the tension in the string. (3)
- (b) By considering the motion of B , find the value of μ . (8)
- (c) Find the resultant force exerted by the string on the pulley, giving its magnitude and direction. (3)



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Question 7 continued

Lined area for answer continuation.

Q7

(Total 14 marks)

TOTAL FOR PAPER: 75 MARKS

END



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6677/01

Edexcel GCE

Mechanics M1

Advanced/Advanced Subsidiary

Tuesday 6 June 2006 – Afternoon

Time: 1 hour 30 minutes

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Team Leader's use only

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1.

Figure 1

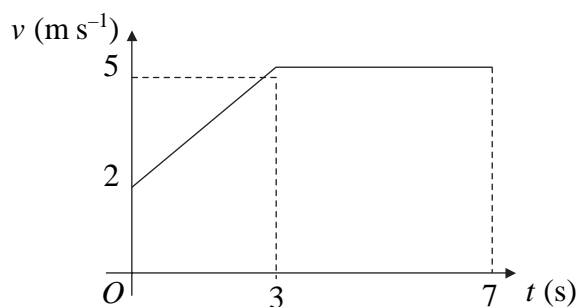


Figure 1 shows the speed-time graph of a cyclist moving on a straight road over a 7 s period. The sections of the graph from $t = 0$ to $t = 3$, and from $t = 3$ to $t = 7$, are straight lines. The section from $t = 3$ to $t = 7$ is parallel to the t -axis.

State what can be deduced about the motion of the cyclist from the fact that

- (a) the graph from $t = 0$ to $t = 3$ is a straight line, (1)

- (b) the graph from $t = 3$ to $t = 7$ is parallel to the t -axis. (1)

- (c) Find the distance travelled by the cyclist during this 7 s period. (4)



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3. A train moves along a straight track with constant acceleration. Three telegraph poles are set at equal intervals beside the track at points *A*, *B* and *C*, where $AB = 50$ m and $BC = 50$ m. The front of the train passes *A* with speed 22.5 m s^{-1} , and 2 s later it passes *B*. Find

(a) the acceleration of the train, (3)

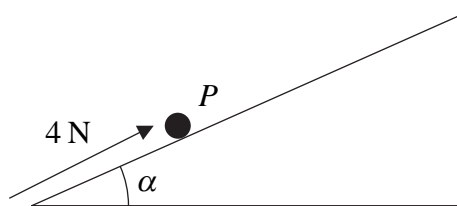
(b) the speed of the front of the train when it passes *C*, (3)

(c) the time that elapses from the instant the front of the train passes *B* to the instant it passes *C*. (4)



4.

Figure 2



A particle P of mass 0.5 kg is on a rough plane inclined at an angle α to the horizontal, where $\tan \alpha = \frac{3}{4}$. The particle is held at rest on the plane by the action of a force of magnitude 4 N acting up the plane in a direction parallel to a line of greatest slope of the plane, as shown in Figure 2. The particle is on the point of slipping up the plane.

(a) Find the coefficient of friction between P and the plane. (7)

The force of magnitude 4 N is removed.

(b) Find the acceleration of P down the plane. (4)

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Question 4 continued

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(Total 11 marks)

Q4

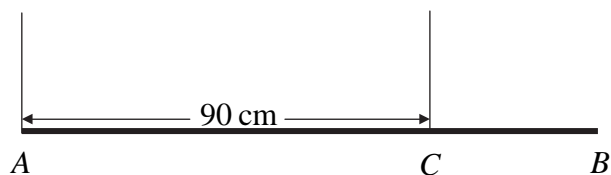
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5.

Figure 3



A steel girder AB has weight 210 N . It is held in equilibrium in a horizontal position by two vertical cables. One cable is attached to the end A . The other cable is attached to the point C on the girder, where $AC = 90 \text{ cm}$, as shown in Figure 3. The girder is modelled as a uniform rod, and the cables as light inextensible strings.

Given that the tension in the cable at C is twice the tension in the cable at A , find

(a) the tension in the cable at A , (2)

(b) show that $AB = 120 \text{ cm}$. (4)

A small load of weight W newtons is attached to the girder at B . The load is modelled as a particle. The girder remains in equilibrium in a horizontal position. The tension in the cable at C is now three times the tension in the cable at A .

(c) Find the value of W . (7)



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6. A car is towing a trailer along a straight horizontal road by means of a horizontal tow-rope. The mass of the car is 1400 kg. The mass of the trailer is 700 kg. The car and the trailer are modelled as particles and the tow-rope as a light inextensible string. The resistances to motion of the car and the trailer are assumed to be constant and of magnitude 630 N and 280 N respectively. The driving force on the car, due to its engine, is 2380 N. Find

(a) the acceleration of the car, **(3)**

(b) the tension in the tow-rope. **(3)**

When the car and trailer are moving at 12 m s^{-1} , the tow-rope breaks. Assuming that the driving force on the car and the resistances to motion are unchanged,

(c) find the distance moved by the car in the first 4 s after the tow-rope breaks. **(6)**

(d) State how you have used the modelling assumption that the tow-rope is inextensible. **(1)**



Leave blank

7. [In this question the unit vectors \mathbf{i} and \mathbf{j} are due east and north respectively.]

A ship S is moving with constant velocity $(-2.5\mathbf{i} + 6\mathbf{j}) \text{ km h}^{-1}$. At time 1200, the position vector of S relative to a fixed origin O is $(16\mathbf{i} + 5\mathbf{j}) \text{ km}$. Find

(a) the speed of S , (2)

(b) the bearing on which S is moving. (2)

The ship is heading directly towards a submerged rock R . A radar tracking station calculates that, if S continues on the same course with the same speed, it will hit R at the time 1500.

(c) Find the position vector of R . (2)

The tracking station warns the ship's captain of the situation. The captain maintains S on its course with the same speed until the time is 1400. He then changes course so that S moves due north at a constant speed of 5 km h^{-1} . Assuming that S continues to move with this new constant velocity, find

(d) an expression for the position vector of the ship t hours after 1400, (4)

(e) the time when S will be due east of R , (2)

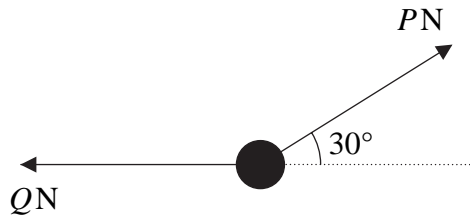
(f) the distance of S from R at the time 1600. (3)



Leave blank

1.

Figure 1



A particle of weight 24 N is held in equilibrium by two light inextensible strings. One string is horizontal. The other string is inclined at an angle of 30° to the horizontal, as shown in Figure 1. The tension in the horizontal string is Q newtons and the tension in the other string is P newtons. Find

(a) the value of P , (3)

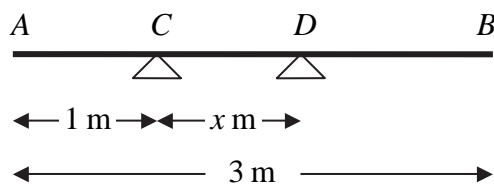
(b) the value of Q . (3)



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2.

Figure 2



A uniform plank *AB* has weight 120 N and length 3 m. The plank rests horizontally in equilibrium on two smooth supports *C* and *D*, where $AC = 1$ m and $CD = x$ m, as shown in Figure 2. The reaction of the support on the plank at *D* has magnitude 80 N. Modelling the plank as a rod,

(a) show that $x = 0.75$ (3)

A rock is now placed at *B* and the plank is on the point of tilting about *D*. Modelling the rock as a particle, find

(b) the weight of the rock, (4)

(c) the magnitude of the reaction of the support on the plank at *D*. (2)

(d) State how you have used the model of the rock as a particle. (1)



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Question 2 continued

Lined area for writing the answer to Question 2.

(Total 10 marks)

Q2

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4. A particle P of mass 0.3 kg is moving with speed $u \text{ m s}^{-1}$ in a straight line on a smooth horizontal table. The particle P collides directly with a particle Q of mass 0.6 kg , which is at rest on the table. Immediately after the particles collide, P has speed 2 m s^{-1} and Q has speed 5 m s^{-1} . The direction of motion of P is reversed by the collision. Find

(a) the value of u , (4)

(b) the magnitude of the impulse exerted by P on Q . (2)

Immediately after the collision, a constant force of magnitude $R \text{ newtons}$ is applied to Q in the direction directly opposite to the direction of motion of Q . As a result Q is brought to rest in 1.5 s .

(c) Find the value of R . (4)



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Question 5 continued

Lined area for answering the question.

(Total 10 marks)

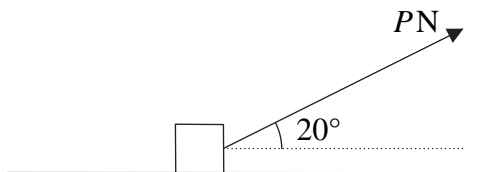
Q5

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6.

Figure 3



A box of mass 30 kg is being pulled along rough horizontal ground at a constant speed using a rope. The rope makes an angle of 20° with the ground, as shown in Figure 3. The coefficient of friction between the box and the ground is 0.4. The box is modelled as a particle and the rope as a light, inextensible string. The tension in the rope is P newtons.

(a) Find the value of P . (8)

The tension in the rope is now increased to 150 N.

(b) Find the acceleration of the box. (6)

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7.

Figure 4

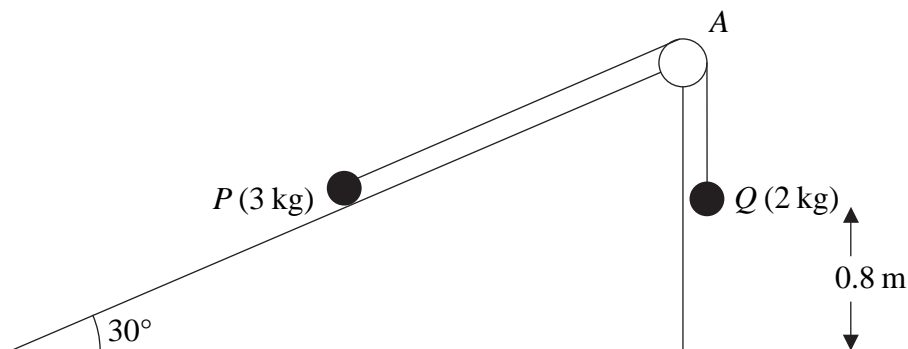


Figure 4 shows two particles P and Q , of mass 3 kg and 2 kg respectively, connected by a light inextensible string. Initially P is held at rest on a fixed smooth plane inclined at 30° to the horizontal. The string passes over a small smooth light pulley A fixed at the top of the plane. The part of the string from P to A is parallel to a line of greatest slope of the plane. The particle Q hangs freely below A . The system is released from rest with the string taut.

(a) Write down an equation of motion for P and an equation of motion for Q . (4)

(b) Hence show that the acceleration of Q is 0.98 m s^{-2} . (2)

(c) Find the tension in the string. (2)

(d) State where in your calculations you have used the information that the string is inextensible. (1)

On release, Q is at a height of 0.8 m above the ground. When Q reaches the ground, it is brought to rest immediately by the impact with the ground and does not rebound. The initial distance of P from A is such that in the subsequent motion P does not reach A . Find

(e) the speed of Q as it reaches the ground, (2)

(f) the time between the instant when Q reaches the ground and the instant when the string becomes taut again. (5)



Centre No.						Paper Reference	Surname	Initial(s)
Candidate No.					6 6 7 7 / 0 1	Signature		

Paper Reference(s)

6677/01

Edexcel GCE

Mechanics M1

Advanced/Advanced Subsidiary

Thursday 7 June 2007 – Morning

Time: 1 hour 30 minutes

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Question Number	Leave Blank
1	
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Total	

<u>Materials required for examination</u>	<u>Items included with question papers</u>
Mathematical Formulae (Green)	Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulas stored in them.

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In the boxes above, write your centre number, candidate number, your surname, initial(s) and signature.

Check that you have the correct question paper.

You must write your answer to each question in the space following the question.

Whenever a numerical value of g is required, take $g = 9.8 \text{ m s}^{-2}$.

When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided.

Full marks may be obtained for answers to ALL questions.

The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).

There are 7 questions in this question paper. The total mark for this paper is 75.

There are 20 pages in this question paper. Any blank pages are indicated.

Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled.

You should show sufficient working to make your methods clear to the Examiner.

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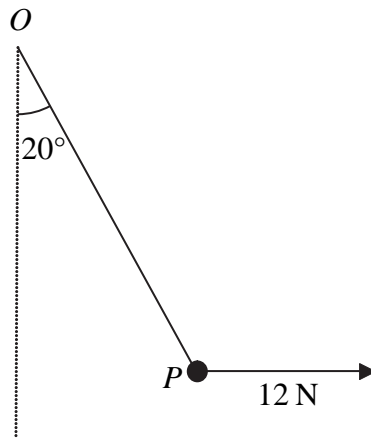


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1.

Figure 1



A particle P is attached to one end of a light inextensible string. The other end of the string is attached to a fixed point O . A horizontal force of magnitude 12 N is applied to P . The particle P is in equilibrium with the string taut and OP making an angle of 20° with the downward vertical, as shown in Figure 1.

Find

(a) the tension in the string, **(3)**

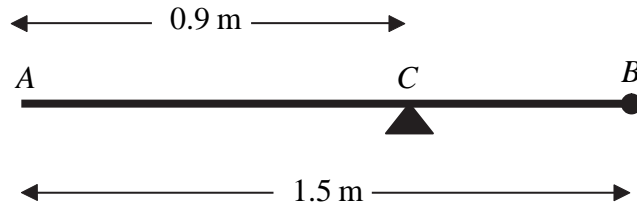
(b) the weight of P . **(4)**



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3.

Figure 2



A uniform rod AB has length 1.5 m and mass 8 kg. A particle of mass m kg is attached to the rod at B . The rod is supported at the point C , where $AC = 0.9$ m, and the system is in equilibrium with AB horizontal, as shown in Figure 2.

(a) Show that $m = 2$. (4)

A particle of mass 5 kg is now attached to the rod at A and the support is moved from C to a point D of the rod. The system, including both particles, is again in equilibrium with AB horizontal.

(b) Find the distance AD . (5)



Leave blank

4. A car is moving along a straight horizontal road. At time $t = 0$, the car passes a point A with speed 25 m s^{-1} . The car moves with constant speed 25 m s^{-1} until $t = 10 \text{ s}$. The car then decelerates uniformly for 8 s . At time $t = 18 \text{ s}$, the speed of the car is $V \text{ m s}^{-1}$ and this speed is maintained until the car reaches the point B at time $t = 30 \text{ s}$.

(a) Sketch, in the space below, a speed–time graph to show the motion of the car from A to B . (3)

Given that $AB = 526 \text{ m}$, find

(b) the value of V , (5)

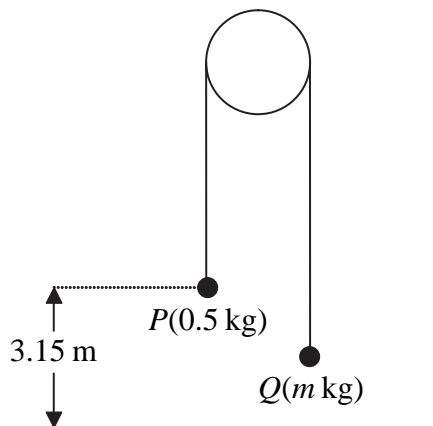
(c) the deceleration of the car between $t = 10 \text{ s}$ and $t = 18 \text{ s}$. (3)



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6.

Figure 4



Two particles P and Q have mass 0.5 kg and $m \text{ kg}$ respectively, where $m < 0.5$. The particles are connected by a light inextensible string which passes over a smooth, fixed pulley. Initially P is 3.15 m above horizontal ground. The particles are released from rest with the string taut and the hanging parts of the string vertical, as shown in Figure 4. After P has been descending for 1.5 s , it strikes the ground. Particle P reaches the ground before Q has reached the pulley.

- (a) Show that the acceleration of P as it descends is 2.8 m s^{-2} . (3)
- (b) Find the tension in the string as P descends. (3)
- (c) Show that $m = \frac{5}{18}$. (4)
- (d) State how you have used the information that the string is inextensible. (1)

When P strikes the ground, P does not rebound and the string becomes slack. Particle Q then moves freely under gravity, without reaching the pulley, until the string becomes taut again.

- (e) Find the time between the instant when P strikes the ground and the instant when the string becomes taut again. (6)



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7. A boat *B* is moving with constant velocity. At noon, *B* is at the point with position vector $(3\mathbf{i} - 4\mathbf{j})$ km with respect to a fixed origin *O*. At 1430 on the same day, *B* is at the point with position vector $(8\mathbf{i} + 11\mathbf{j})$ km.

- (a) Find the velocity of *B*, giving your answer in the form $p\mathbf{i} + q\mathbf{j}$. (3)

At time *t* hours after noon, the position vector of *B* is **b** km.

- (b) Find, in terms of *t*, an expression for **b**. (3)

Another boat *C* is also moving with constant velocity. The position vector of *C*, **c** km, at time *t* hours after noon, is given by

$$\mathbf{c} = (-9\mathbf{i} + 20\mathbf{j}) + t(6\mathbf{i} + \lambda\mathbf{j}),$$

where λ is a constant. Given that *C* intercepts *B*,

- (c) find the value of λ , (5)

- (d) show that, before *C* intercepts *B*, the boats are moving with the same speed. (3)



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Question 7 continued

Ruled lines for writing the answer to Question 7.

Q7

(Total 14 marks)

TOTAL FOR PAPER: 75 MARKS

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1. Two particles A and B have masses 4 kg and $m \text{ kg}$ respectively. They are moving towards each other in opposite directions on a smooth horizontal table when they collide directly. Immediately before the collision, the speed of A is 5 m s^{-1} and the speed of B is 3 m s^{-1} . Immediately after the collision, the direction of motion of A is unchanged and the speed of A is 1 m s^{-1} .

(a) Find the magnitude of the impulse exerted on A in the collision. **(2)**

Immediately after the collision, the speed of B is 2 m s^{-1} .

(b) Find the value of m . **(4)**



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2. A firework rocket starts from rest at ground level and moves vertically. In the first 3 s of its motion, the rocket rises 27 m. The rocket is modelled as a particle moving with constant acceleration $a \text{ m s}^{-2}$. Find

(a) the value of a , (2)

(b) the speed of the rocket 3 s after it has left the ground. (2)

After 3 s, the rocket burns out. The motion of the rocket is now modelled as that of a particle moving freely under gravity.

(c) Find the height of the rocket above the ground 5 s after it has left the ground. (4)



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3. A car moves along a horizontal straight road, passing two points A and B . At A the speed of the car is 15 m s^{-1} . When the driver passes A , he sees a warning sign W ahead of him, 120 m away. He immediately applies the brakes and the car decelerates with uniform deceleration, reaching W with speed 5 m s^{-1} . At W , the driver sees that the road is clear. He then immediately accelerates the car with uniform acceleration for 16 s to reach a speed of $V \text{ m s}^{-1}$ ($V > 15$). He then maintains the car at a constant speed of $V \text{ m s}^{-1}$. Moving at this constant speed, the car passes B after a further 22 s .

(a) Sketch, in the space below, a speed-time graph to illustrate the motion of the car as it moves from A to B .

(3)

(b) Find the time taken for the car to move from A to B .

(3)

The distance from A to B is 1 km .

(c) Find the value of V .

(5)



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4.

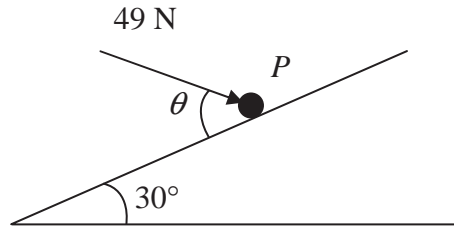


Figure 1

A particle P of mass 6 kg lies on the surface of a smooth plane. The plane is inclined at an angle of 30° to the horizontal. The particle is held in equilibrium by a force of magnitude 49 N , acting at an angle θ to the plane, as shown in Figure 1. The force acts in a vertical plane through a line of greatest slope of the plane.

(a) Show that $\cos \theta = \frac{3}{5}$. (3)

(b) Find the normal reaction between P and the plane. (4)

The direction of the force of magnitude 49 N is now changed. It is now applied horizontally to P so that P moves up the plane. The force again acts in a vertical plane through a line of greatest slope of the plane.

(c) Find the initial acceleration of P . (4)



5.

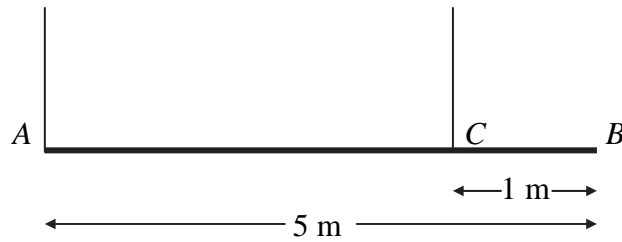


Figure 2

A beam AB has mass 12 kg and length 5 m. It is held in equilibrium in a horizontal position by two vertical ropes attached to the beam. One rope is attached to A , the other to the point C on the beam, where $BC = 1$ m, as shown in Figure 2. The beam is modelled as a uniform rod, and the ropes as light strings.

- (a) Find
- (i) the tension in the rope at C ,
 - (ii) the tension in the rope at A .
- (5)**

A small load of mass 16 kg is attached to the beam at a point which is y metres from A . The load is modelled as a particle. Given that the beam remains in equilibrium in a horizontal position,

- (b) find, in terms of y , an expression for the tension in the rope at C .
- (3)**

The rope at C will break if its tension exceeds 98 N. The rope at A cannot break.

- (c) Find the range of possible positions on the beam where the load can be attached without the rope at C breaking.
- (3)**



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6. [In this question, the unit vectors \mathbf{i} and \mathbf{j} are due east and due north respectively.]

A particle P is moving with constant velocity $(-5\mathbf{i} + 8\mathbf{j}) \text{ m s}^{-1}$. Find

(a) the speed of P , (2)

(b) the direction of motion of P , giving your answer as a bearing. (3)

At time $t = 0$, P is at the point A with position vector $(7\mathbf{i} - 10\mathbf{j}) \text{ m}$ relative to a fixed origin O . When $t = 3 \text{ s}$, the velocity of P changes and it moves with velocity $(u\mathbf{i} + v\mathbf{j}) \text{ m s}^{-1}$, where u and v are constants. After a further 4 s , it passes through O and continues to move with velocity $(u\mathbf{i} + v\mathbf{j}) \text{ m s}^{-1}$.

(c) Find the values of u and v . (5)

(d) Find the total time taken for P to move from A to a position which is due south of A . (3)

Horizontal lines for writing answers.



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7.



Figure 3

Two particles *A* and *B*, of mass *m* and *2m* respectively, are attached to the ends of a light inextensible string. The particle *A* lies on a rough horizontal table. The string passes over a small smooth pulley *P* fixed on the edge of the table. The particle *B* hangs freely below the pulley, as shown in Figure 3. The coefficient of friction between *A* and the table is μ . The particles are released from rest with the string taut. Immediately after release, the magnitude of the acceleration of *A* and *B* is $\frac{4}{9}g$. By writing down separate equations of motion for *A* and *B*,

(a) find the tension in the string immediately after the particles begin to move, (3)

(b) show that $\mu = \frac{2}{3}$. (5)

When *B* has fallen a distance *h*, it hits the ground and does not rebound. Particle *A* is then a distance $\frac{1}{3}h$ from *P*.

(c) Find the speed of *A* as it reaches *P*. (6)

(d) State how you have used the information that the string is light. (1)



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3. A particle P of mass 0.4 kg moves under the action of a single constant force \mathbf{F} newtons. The acceleration of P is $(6\mathbf{i} + 8\mathbf{j}) \text{ m s}^{-2}$. Find

(a) the angle between the acceleration and \mathbf{i} , (2)

(b) the magnitude of \mathbf{F} . (3)

At time t seconds the velocity of P is $\mathbf{v} \text{ m s}^{-1}$. Given that when $t = 0$, $\mathbf{v} = 9\mathbf{i} - 10\mathbf{j}$,

(c) find the velocity of P when $t = 5$. (3)



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4. A car is moving along a straight horizontal road. The speed of the car as it passes the point A is 25 m s^{-1} and the car maintains this speed for 30 s . The car then decelerates uniformly to a speed of 10 m s^{-1} . The speed of 10 m s^{-1} is then maintained until the car passes the point B . The time taken to travel from A to B is 90 s and $AB = 1410 \text{ m}$.

(a) Sketch, in the space below, a speed-time graph to show the motion of the car from A to B . (2)

(b) Calculate the deceleration of the car as it decelerates from 25 m s^{-1} to 10 m s^{-1} . (7)



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Question 4 continued

Q4

(Total 9 marks)



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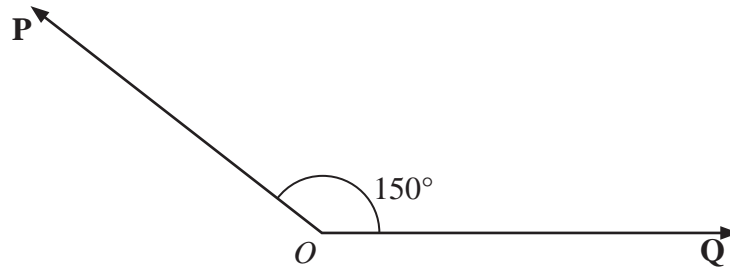


Figure 1

Two forces **P** and **Q** act on a particle at a point *O*. The force **P** has magnitude 15 N and the force **Q** has magnitude *X* newtons. The angle between **P** and **Q** is 150° , as shown in Figure 1. The resultant of **P** and **Q** is **R**.

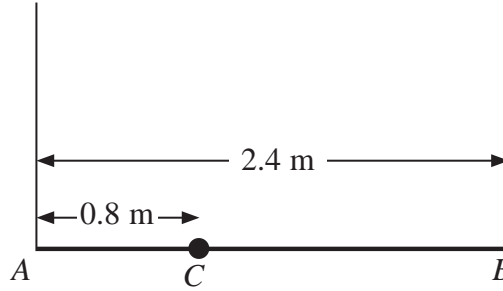
Given that the angle between **R** and **Q** is 50° , find

(a) the magnitude of **R**, **(4)**

(b) the value of *X*. **(5)**



6.

**Figure 2**

A plank AB has mass 12 kg and length 2.4 m . A load of mass 8 kg is attached to the plank at the point C , where $AC = 0.8 \text{ m}$. The loaded plank is held in equilibrium, with AB horizontal, by two vertical ropes, one attached at A and the other attached at B , as shown in Figure 2. The plank is modelled as a uniform rod, the load as a particle and the ropes as light inextensible strings.

- (a) Find the tension in the rope attached at B . (4)

The plank is now modelled as a non-uniform rod. With the new model, the tension in the rope attached at A is 10 N greater than the tension in the rope attached at B .

- (b) Find the distance of the centre of mass of the plank from A . (6)



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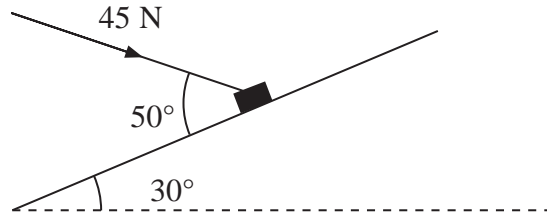


Figure 3

A package of mass 4 kg lies on a rough plane inclined at 30° to the horizontal. The package is held in equilibrium by a force of magnitude 45 N acting at an angle of 50° to the plane, as shown in Figure 3. The force is acting in a vertical plane through a line of greatest slope of the plane. The package is in equilibrium on the point of moving up the plane. The package is modelled as a particle. Find

- (a) the magnitude of the normal reaction of the plane on the package, (5)

- (b) the coefficient of friction between the plane and the package. (6)



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Question 7 continued _____

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8.



Figure 4

Two particles P and Q , of mass 2 kg and 3 kg respectively, are joined by a light inextensible string. Initially the particles are at rest on a rough horizontal plane with the string taut. A constant force \mathbf{F} of magnitude 30 N is applied to Q in the direction PQ , as shown in Figure 4. The force is applied for 3 s and during this time Q travels a distance of 6 m. The coefficient of friction between each particle and the plane is μ . Find

- (a) the acceleration of Q , (2)
- (b) the value of μ , (4)
- (c) the tension in the string. (4)
- (d) State how in your calculation you have used the information that the string is inextensible. (1)

When the particles have moved for 3 s, the force \mathbf{F} is removed.

- (e) Find the time between the instant that the force is removed and the instant that Q comes to rest. (4)



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Question 8 continued

Q8

(Total 15 marks)

TOTAL FOR PAPER: 75 MARKS

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Candidate No.						6 6 7 7 / 0 1		

Paper Reference(s)

6677/01

Edexcel GCE

Mechanics M1

Advanced/Advanced Subsidiary

Tuesday 13 January 2009 – Morning

Time: 1 hour 30 minutes

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Team Leader’s use only

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Question Number	Leave Blank
1	
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Materials required for examination
Mathematical Formulae (Green)

Items included with question papers
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2. A small ball is projected vertically upwards from ground level with speed $u \text{ m s}^{-1}$. The ball takes 4 s to return to ground level.

(a) Draw, in the space below, a velocity-time graph to represent the motion of the ball during the first 4 s.

(2)

(b) The maximum height of the ball above the ground during the first 4 s is 19.6 m. Find the value of u .

(3)



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3. Two particles *A* and *B* are moving on a smooth horizontal plane. The mass of *A* is *km*, where $2 < k < 3$, and the mass of *B* is *m*. The particles are moving along the same straight line, but in opposite directions, and they collide directly. Immediately before they collide the speed of *A* is $2u$ and the speed of *B* is $4u$. As a result of the collision the speed of *A* is halved and its direction of motion is reversed.

(a) Find, in terms of *k* and *u*, the speed of *B* immediately after the collision. (3)

(b) State whether the direction of motion of *B* changes as a result of the collision, explaining your answer. (3)

Given that $k = \frac{7}{3}$,

(c) find, in terms of *m* and *u*, the magnitude of the impulse that *A* exerts on *B* in the collision. (3)



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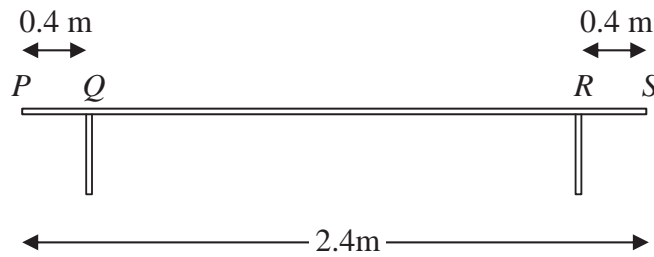


Figure 1

A bench consists of a plank which is resting in a horizontal position on two thin vertical legs. The plank is modelled as a uniform rod PS of length 2.4 m and mass 20 kg. The legs at Q and R are 0.4 m from each end of the plank, as shown in Figure 1.

Two pupils, Arthur and Beatrice, sit on the plank. Arthur has mass 60 kg and sits at the middle of the plank and Beatrice has mass 40 kg and sits at the end P . The plank remains horizontal and in equilibrium. By modelling the pupils as particles, find

- (a) the magnitude of the normal reaction between the plank and the leg at Q and the magnitude of the normal reaction between the plank and the leg at R . (7)

Beatrice stays sitting at P but Arthur now moves and sits on the plank at the point X . Given that the plank remains horizontal and in equilibrium, and that the magnitude of the normal reaction between the plank and the leg at Q is now twice the magnitude of the normal reaction between the plank and the leg at R ,

- (b) find the distance QX . (6)



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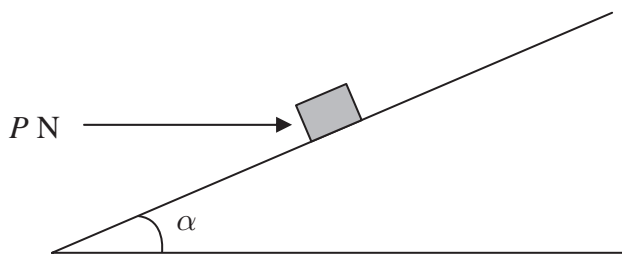


Figure 2

A small package of mass 1.1 kg is held in equilibrium on a rough plane by a horizontal force. The plane is inclined at an angle α to the horizontal, where $\tan \alpha = \frac{3}{4}$. The force acts in a vertical plane containing a line of greatest slope of the plane and has magnitude P newtons, as shown in Figure 2.

The coefficient of friction between the package and the plane is 0.5 and the package is modelled as a particle. The package is in equilibrium and on the point of slipping down the plane.

(a) Draw, on Figure 2, all the forces acting on the package, showing their directions clearly. (2)

(b) (i) Find the magnitude of the normal reaction between the package and the plane.

(ii) Find the value of P . (11)



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6. Two forces, $(4\mathbf{i} - 5\mathbf{j})$ N and $(p\mathbf{i} + q\mathbf{j})$ N, act on a particle P of mass m kg. The resultant of the two forces is \mathbf{R} . Given that \mathbf{R} acts in a direction which is parallel to the vector $(\mathbf{i} - 2\mathbf{j})$,

(a) find the angle between \mathbf{R} and the vector \mathbf{j} , (3)

(b) show that $2p + q + 3 = 0$. (4)

Given also that $q = 1$ and that P moves with an acceleration of magnitude $8\sqrt{5} \text{ m s}^{-2}$,

(c) find the value of m . (7)



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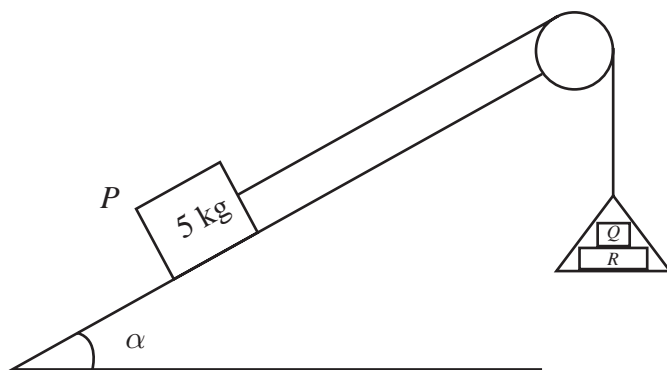


Figure 3

One end of a light inextensible string is attached to a block P of mass 5 kg . The block P is held at rest on a smooth fixed plane which is inclined to the horizontal at an angle α , where $\sin \alpha = \frac{3}{5}$. The string lies along a line of greatest slope of the plane and passes over a smooth light pulley which is fixed at the top of the plane. The other end of the string is attached to a light scale pan which carries two blocks Q and R , with block Q on top of block R , as shown in Figure 3. The mass of block Q is 5 kg and the mass of block R is 10 kg . The scale pan hangs at rest and the system is released from rest. By modelling the blocks as particles, ignoring air resistance and assuming the motion is uninterrupted, find

- (a) (i) the acceleration of the scale pan,
 - (ii) the tension in the string, (8)
- (b) the magnitude of the force exerted on block Q by block R , (3)
- (c) the magnitude of the force exerted on the pulley by the string. (5)



Centre No.						Paper Reference					Surname	Initial(s)
						6	6	7	7	/	0	1

Paper Reference(s)

6677/01

Edexcel GCE

Mechanics M1

Advanced/Advanced Subsidiary

Friday 22 May 2009 – Morning

Time: 1 hour 30 minutes

Examiner's use only

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Team Leader's use only

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Question Number	Leave Blank
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Total	

Materials required for examination

Mathematical Formulae (Orange or Green)

Items included with question papers

Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.
 Answer **ALL** the questions.
 You must write your answer to each question in the space following the question.
 If you need more space to complete your answer to any question, use additional answer sheets.
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2. A particle is acted upon by two forces \mathbf{F}_1 and \mathbf{F}_2 , given by

$$\mathbf{F}_1 = (i - 3j) \text{ N,}$$

$$\mathbf{F}_2 = (pi + 2pj) \text{ N, where } p \text{ is a positive constant.}$$

(a) Find the angle between \mathbf{F}_2 and \mathbf{j} .

(2)

The resultant of \mathbf{F}_1 and \mathbf{F}_2 is \mathbf{R} . Given that \mathbf{R} is parallel to \mathbf{i} ,

(b) find the value of p .

(4)



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3. Two particles A and B are moving on a smooth horizontal plane. The mass of A is $2m$ and the mass of B is m . The particles are moving along the same straight line but in opposite directions and they collide directly. Immediately before they collide the speed of A is $2u$ and the speed of B is $3u$. The magnitude of the impulse received by each particle in the collision is $\frac{7mu}{2}$.

Find

(a) the speed of A immediately after the collision, (3)

(b) the speed of B immediately after the collision. (3)



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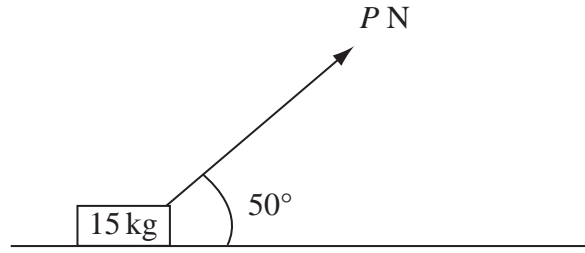


Figure 1

A small box of mass 15 kg rests on a rough horizontal plane. The coefficient of friction between the box and the plane is 0.2. A force of magnitude P newtons is applied to the box at 50° to the horizontal, as shown in Figure 1. The box is on the point of sliding along the plane.

Find the value of P , giving your answer to 2 significant figures.

(9)



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6. A car of mass 800 kg pulls a trailer of mass 200 kg along a straight horizontal road using a light towbar which is parallel to the road. The horizontal resistances to motion of the car and the trailer have magnitudes 400 N and 200 N respectively. The engine of the car produces a constant horizontal driving force on the car of magnitude 1200 N. Find

(a) the acceleration of the car and trailer, (3)

(b) the magnitude of the tension in the towbar. (3)

The car is moving along the road when the driver sees a hazard ahead. He reduces the force produced by the engine to zero and applies the brakes. The brakes produce a force on the car of magnitude F newtons and the car and trailer decelerate. Given that the resistances to motion are unchanged and the magnitude of the thrust in the towbar is 100 N,

(c) find the value of F . (7)



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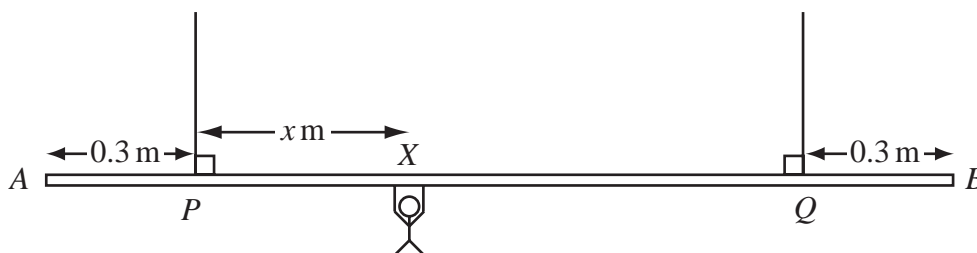


Figure 2

A beam AB is supported by two vertical ropes, which are attached to the beam at points P and Q , where $AP = 0.3$ m and $BQ = 0.3$ m. The beam is modelled as a uniform rod, of length 2 m and mass 20 kg. The ropes are modelled as light inextensible strings. A gymnast of mass 50 kg hangs on the beam between P and Q . The gymnast is modelled as a particle attached to the beam at the point X , where $PX = x$ m, $0 < x < 1.4$ as shown in Figure 2. The beam rests in equilibrium in a horizontal position.

(a) Show that the tension in the rope attached to the beam at P is $(588 - 350x)$ N. (3)

(b) Find, in terms of x , the tension in the rope attached to the beam at Q . (3)

(c) Hence find, justifying your answer carefully, the range of values of the tension which could occur in each rope. (3)

Given that the tension in the rope attached at Q is three times the tension in the rope attached at P ,

(d) find the value of x . (3)



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8. [In this question \mathbf{i} and \mathbf{j} are horizontal unit vectors due east and due north respectively.]

A hiker H is walking with constant velocity $(1.2\mathbf{i} - 0.9\mathbf{j}) \text{ m s}^{-1}$.

(a) Find the speed of H . (2)

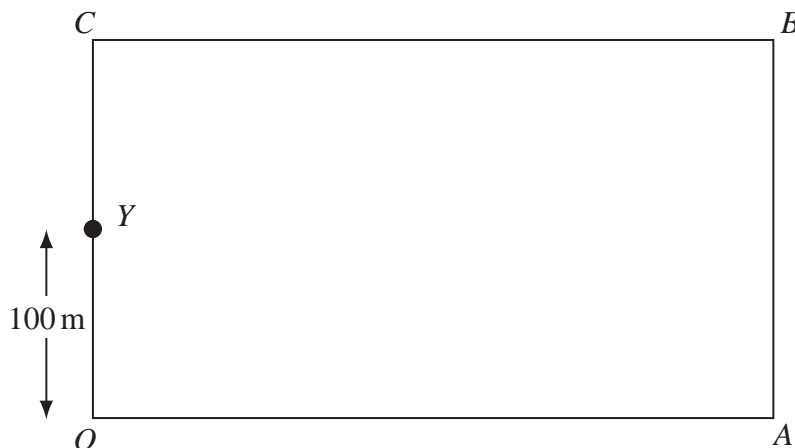


Figure 3

A horizontal field $OABC$ is rectangular with OA due east and OC due north, as shown in Figure 3. At twelve noon hiker H is at the point Y with position vector $100\mathbf{j}$ m, relative to the fixed origin O .

(b) Write down the position vector of H at time t seconds after noon. (2)

At noon, another hiker K is at the point with position vector $(9\mathbf{i} + 46\mathbf{j})$ m. Hiker K is moving with constant velocity $(0.75\mathbf{i} + 1.8\mathbf{j}) \text{ m s}^{-1}$.

(c) Show that, at time t seconds after noon,

$$\overrightarrow{HK} = [(9 - 0.45t)\mathbf{i} + (2.7t - 54)\mathbf{j}] \text{ metres.} \quad (4)$$

Hence,

(d) show that the two hikers meet and find the position vector of the point where they meet. (5)



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1. A particle *A* of mass 2 kg is moving along a straight horizontal line with speed 12 m s^{-1} . Another particle *B* of mass m kg is moving along the same straight line, in the opposite direction to *A*, with speed 8 m s^{-1} . The particles collide. The direction of motion of *A* is unchanged by the collision. Immediately after the collision, *A* is moving with speed 3 m s^{-1} and *B* is moving with speed 4 m s^{-1} . Find
- (a) the magnitude of the impulse exerted by *B* on *A* in the collision, (2)

 - (b) the value of m . (4)



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2. An athlete runs along a straight road. She starts from rest and moves with constant acceleration for 5 seconds, reaching a speed of 8 m s^{-1} . This speed is then maintained for T seconds. She then decelerates at a constant rate until she stops. She has run a total of 500 m in 75 s.

(a) In the space below, sketch a speed-time graph to illustrate the motion of the athlete. (3)

(b) Calculate the value of T . (5)



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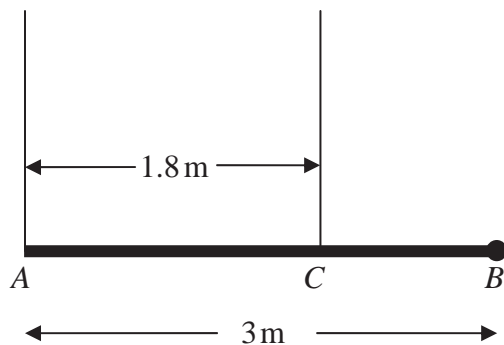


Figure 2

A pole AB has length 3 m and weight W newtons. The pole is held in a horizontal position in equilibrium by two vertical ropes attached to the pole at the points A and C where $AC = 1.8$ m, as shown in Figure 2. A load of weight 20 N is attached to the rod at B . The pole is modelled as a uniform rod, the ropes as light inextensible strings and the load as a particle.

(a) Show that the tension in the rope attached to the pole at C is $\left(\frac{5}{6}W + \frac{100}{3}\right)$ N. (4)

(b) Find, in terms of W , the tension in the rope attached to the pole at A . (3)

Given that the tension in the rope attached to the pole at C is eight times the tension in the rope attached to the pole at A ,

(c) find the value of W . (3)



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Question 4 continued

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5. A particle of mass 0.8 kg is held at rest on a rough plane. The plane is inclined at 30° to the horizontal. The particle is released from rest and slides down a line of greatest slope of the plane. The particle moves 2.7 m during the first 3 seconds of its motion. Find

(a) the acceleration of the particle, (3)

(b) the coefficient of friction between the particle and the plane. (5)

The particle is now held on the same rough plane by a horizontal force of magnitude X newtons, acting in a plane containing a line of greatest slope of the plane, as shown in Figure 3. The particle is in equilibrium and on the point of moving up the plane.

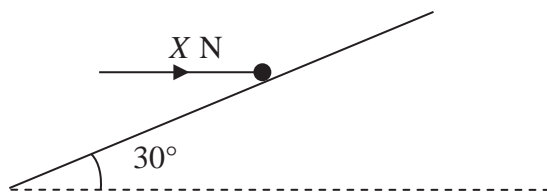


Figure 3

(c) Find the value of X . (7)



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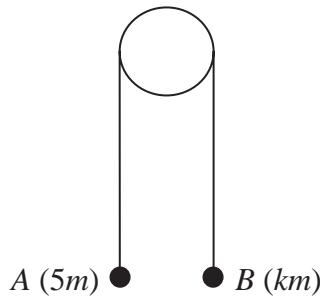


Figure 4

Two particles *A* and *B* have masses $5m$ and km respectively, where $k < 5$. The particles are connected by a light inextensible string which passes over a smooth light fixed pulley. The system is held at rest with the string taut, the hanging parts of the string vertical and with *A* and *B* at the same height above a horizontal plane, as shown in Figure 4. The system is released from rest. After release, *A* descends with acceleration $\frac{1}{4}g$.

(a) Show that the tension in the string as *A* descends is $\frac{15}{4}mg$. (3)

(b) Find the value of *k*. (3)

(c) State how you have used the information that the pulley is smooth. (1)

After descending for 1.2s, the particle *A* reaches the plane. It is immediately brought to rest by the impact with the plane. The initial distance between *B* and the pulley is such that, in the subsequent motion, *B* does not reach the pulley.

(d) Find the greatest height reached by *B* above the plane. (7)



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7. *[In this question, i and j are horizontal unit vectors due east and due north respectively and position vectors are given with respect to a fixed origin.]*

A ship *S* is moving along a straight line with constant velocity. At time *t* hours the position vector of *S* is **s** km. When *t* = 0, **s** = 9**i** − 6**j**. When *t* = 4, **s** = 21**i** + 10**j**. Find

- (a) the speed of *S*, **(4)**
- (b) the direction in which *S* is moving, giving your answer as a bearing. **(2)**
- (c) Show that **s** = (3*t* + 9)**i** + (4*t* − 6)**j**. **(2)**

A lighthouse *L* is located at the point with position vector (18**i** + 6**j**) km. When *t* = *T*, the ship *S* is 10 km from *L*.

- (d) Find the possible values of *T*. **(6)**



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5. Two cars P and Q are moving in the same direction along the same straight horizontal road. Car P is moving with constant speed 25 m s^{-1} . At time $t = 0$, P overtakes Q which is moving with constant speed 20 m s^{-1} . From $t = T$ seconds, P decelerates uniformly, coming to rest at a point X which is 800 m from the point where P overtook Q . From $t = 25 \text{ s}$, Q decelerates uniformly, coming to rest at the same point X at the same instant as P .

(a) Sketch, on the same axes, the speed-time graphs of the two cars for the period from $t = 0$ to the time when they both come to rest at the point X . (4)

(b) Find the value of T . (8)



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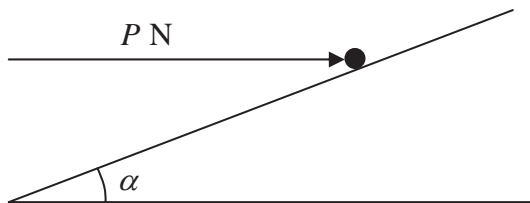


Figure 2

A particle of mass 0.4 kg is held at rest on a fixed rough plane by a horizontal force of magnitude P newtons. The force acts in the vertical plane containing the line of greatest slope of the inclined plane which passes through the particle. The plane is inclined to the horizontal at an angle α , where $\tan \alpha = \frac{3}{4}$, as shown in Figure 2.

The coefficient of friction between the particle and the plane is $\frac{1}{3}$.

Given that the particle is on the point of sliding up the plane, find

(a) the magnitude of the normal reaction between the particle and the plane, (5)

(b) the value of P . (5)



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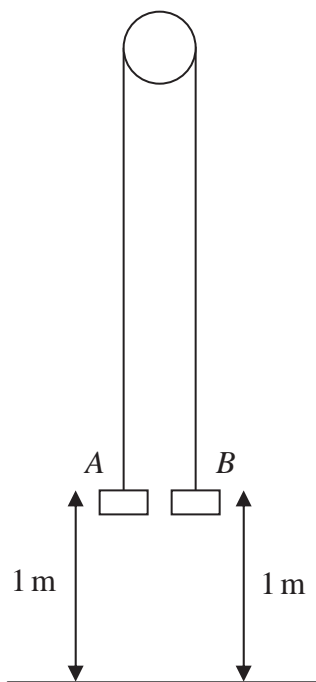


Figure 3

Two particles *A* and *B* have mass 0.4 kg and 0.3 kg respectively. The particles are attached to the ends of a light inextensible string. The string passes over a small smooth pulley which is fixed above a horizontal floor. Both particles are held, with the string taut, at a height of 1 m above the floor, as shown in Figure 3. The particles are released from rest and in the subsequent motion *B* does not reach the pulley.

- (a) Find the tension in the string immediately after the particles are released. (6)
- (b) Find the acceleration of *A* immediately after the particles are released. (2)

When the particles have been moving for 0.5 s, the string breaks.

- (c) Find the further time that elapses until *B* hits the floor. (9)



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1. Two particles B and C have mass m kg and 3 kg respectively. They are moving towards each other in opposite directions on a smooth horizontal table. The two particles collide directly. Immediately before the collision, the speed of B is 4 m s^{-1} and the speed of C is 2 m s^{-1} . In the collision the direction of motion of C is reversed and the direction of motion of B is unchanged. Immediately after the collision, the speed of B is 1 m s^{-1} and the speed of C is 3 m s^{-1} .

Find

- (a) the value of m , (3)

- (b) the magnitude of the impulse received by C . (2)



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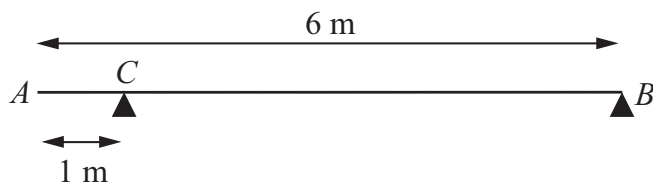


Figure 1

A uniform beam AB has mass 20 kg and length 6 m. The beam rests in equilibrium in a horizontal position on two smooth supports. One support is at C , where $AC = 1$ m, and the other is at the end B , as shown in Figure 1. The beam is modelled as a rod.

(a) Find the magnitudes of the reactions on the beam at B and at C . (5)

A boy of mass 30 kg stands on the beam at the point D . The beam remains in equilibrium. The magnitudes of the reactions on the beam at B and at C are now equal. The boy is modelled as a particle.

(b) Find the distance AD . (5)



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5. A car accelerates uniformly from rest for 20 seconds. It moves at constant speed $v \text{ m s}^{-1}$ for the next 40 seconds and then decelerates uniformly for 10 seconds until it comes to rest.

(a) For the motion of the car, sketch

(i) a speed-time graph,

(ii) an acceleration-time graph.

(6)

Given that the total distance moved by the car is 880 m,

(b) find the value of v .

(4)



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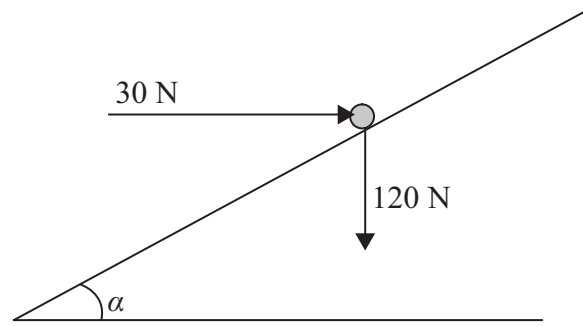


Figure 2

A particle of weight 120 N is placed on a fixed rough plane which is inclined at an angle α to the horizontal, where $\tan \alpha = \frac{3}{4}$.

The coefficient of friction between the particle and the plane is $\frac{1}{2}$.

The particle is held at rest in equilibrium by a horizontal force of magnitude 30 N, which acts in the vertical plane containing the line of greatest slope of the plane through the particle, as shown in Figure 2.

- (a) Show that the normal reaction between the particle and the plane has magnitude 114 N. **(4)**

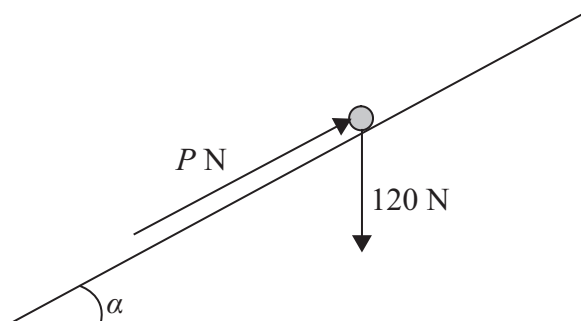


Figure 3

The horizontal force is removed and replaced by a force of magnitude P newtons acting up the slope along the line of greatest slope of the plane through the particle, as shown in Figure 3. The particle remains in equilibrium.

- (b) Find the greatest possible value of P . **(8)**
- (c) Find the magnitude and direction of the frictional force acting on the particle when $P = 30$. **(3)**



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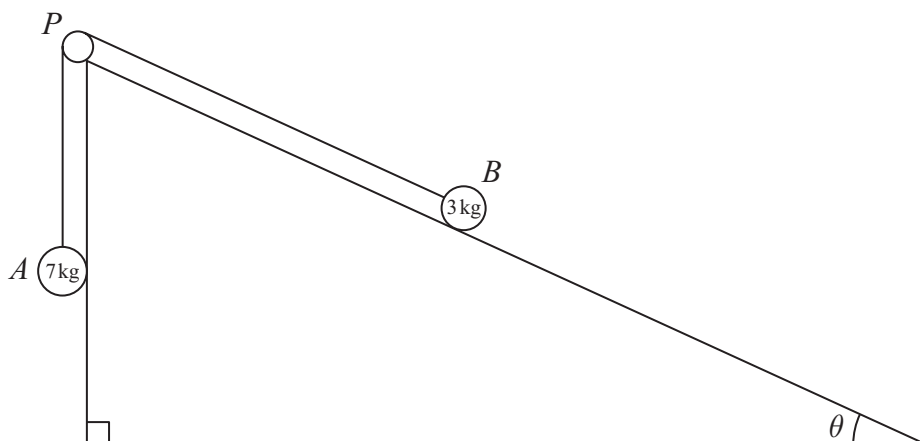


Figure 4

Two particles A and B , of mass 7 kg and 3 kg respectively, are attached to the ends of a light inextensible string. Initially B is held at rest on a rough fixed plane inclined at angle θ to the horizontal, where $\tan \theta = \frac{5}{12}$. The part of the string from B to P is parallel to a line of greatest slope of the plane. The string passes over a small smooth pulley, P , fixed at the top of the plane. The particle A hangs freely below P , as shown in Figure 4. The coefficient of friction between B and the plane is $\frac{2}{3}$. The particles are released from rest with the string taut and B moves up the plane.

(a) Find the magnitude of the acceleration of B immediately after release. (10)

(b) Find the speed of B when it has moved 1 m up the plane. (2)

When B has moved 1 m up the plane the string breaks. Given that in the subsequent motion B does not reach P ,

(c) find the time between the instants when the string breaks and when B comes to instantaneous rest. (4)



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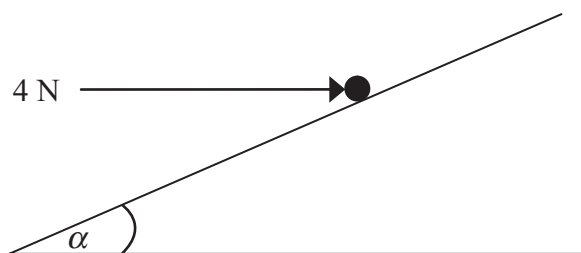


Figure 1

A particle of weight W newtons is held in equilibrium on a rough inclined plane by a horizontal force of magnitude 4 N. The force acts in a vertical plane containing a line of greatest slope of the inclined plane. The plane is inclined to the horizontal at an angle α , where $\tan \alpha = \frac{3}{4}$, as shown in Figure 1.

The coefficient of friction between the particle and the plane is $\frac{1}{2}$.

Given that the particle is on the point of sliding down the plane,

- (i) show that the magnitude of the normal reaction between the particle and the plane is 20 N,
- (ii) find the value of W .

(9)



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4. A girl runs a 400 m race in a time of 84 s. In a model of this race, it is assumed that, starting from rest, she moves with constant acceleration for 4 s, reaching a speed of 5 m s^{-1} . She maintains this speed for 60 s and then moves with constant deceleration for 20 s, crossing the finishing line with a speed of $V \text{ m s}^{-1}$.
- (a) Sketch, in the space below, a speed-time graph for the motion of the girl during the whole race. (2)
- (b) Find the distance run by the girl in the first 64 s of the race. (3)
- (c) Find the value of V . (5)
- (d) Find the deceleration of the girl in the final 20 s of her race. (2)



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5. A plank PQR , of length 8 m and mass 20 kg, is in equilibrium in a horizontal position on two supports at P and Q , where $PQ = 6$ m.

A child of mass 40 kg stands on the plank at a distance of 2 m from P and a block of mass M kg is placed on the plank at the end R . The plank remains horizontal and in equilibrium. The force exerted on the plank by the support at P is equal to the force exerted on the plank by the support at Q .

By modelling the plank as a uniform rod, and the child and the block as particles,

- (a) (i) find the magnitude of the force exerted on the plank by the support at P ,
 (ii) find the value of M . (10)
- (b) State how, in your calculations, you have used the fact that the child and the block can be modelled as particles. (1)



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Question 5 continued

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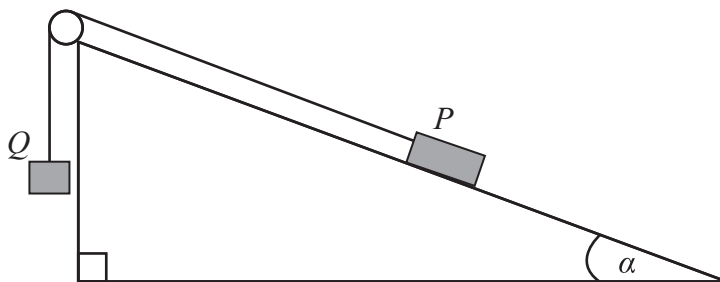


Figure 2

Two particles P and Q have masses 0.3 kg and $m \text{ kg}$ respectively. The particles are attached to the ends of a light inextensible string. The string passes over a small smooth pulley which is fixed at the top of a fixed rough plane. The plane is inclined to the horizontal at an angle α , where $\tan \alpha = \frac{3}{4}$. The coefficient of friction between P and the plane is $\frac{1}{2}$.

The string lies in a vertical plane through a line of greatest slope of the inclined plane. The particle P is held at rest on the inclined plane and the particle Q hangs freely below the pulley with the string taut, as shown in Figure 2.

The system is released from rest and Q accelerates vertically downwards at 1.4 m s^{-2} . Find

- (a) the magnitude of the normal reaction of the inclined plane on P , (2)
- (b) the value of m . (8)

When the particles have been moving for 0.5 s , the string breaks. Assuming that P does not reach the pulley,

- (c) find the further time that elapses until P comes to instantaneous rest. (6)



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7. [In this question \mathbf{i} and \mathbf{j} are unit vectors due east and due north respectively. Position vectors are given relative to a fixed origin O .]

Two ships P and Q are moving with constant velocities. Ship P moves with velocity $(2\mathbf{i} - 3\mathbf{j}) \text{ km h}^{-1}$ and ship Q moves with velocity $(3\mathbf{i} + 4\mathbf{j}) \text{ km h}^{-1}$.

(a) Find, to the nearest degree, the bearing on which Q is moving. (2)

At 2 pm, ship P is at the point with position vector $(\mathbf{i} + \mathbf{j}) \text{ km}$ and ship Q is at the point with position vector $(-2\mathbf{j}) \text{ km}$.

At time t hours after 2 pm, the position vector of P is $\mathbf{p} \text{ km}$ and the position vector of Q is $\mathbf{q} \text{ km}$.

(b) Write down expressions, in terms of t , for
(i) \mathbf{p} ,
(ii) \mathbf{q} ,
(iii) \overrightarrow{PQ} . (5)

(c) Find the time when
(i) Q is due north of P ,
(ii) Q is north-west of P . (4)

Horizontal lines for writing answers.



Centre No.						Paper Reference	Surname	Initial(s)
Candidate No.						6 6 7 7 / 0 1	Signature	

Paper Reference(s)

6677/01

Edexcel GCE

Mechanics M1

Advanced/Advanced Subsidiary

Friday 20 January 2012 – Afternoon

Time: 1 hour 30 minutes

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Materials required for examination

Mathematical Formulae (Pink)

Items included with question papers

Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation or symbolic differentiation/integration, or have retrievable mathematical formulae stored in them.

Question Number	Leave Blank
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Instructions to Candidates

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There are 8 questions in this question paper. The total mark for this paper is 75.

There are 28 pages in this question paper. Any blank pages are indicated.

Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled.

You should show sufficient working to make your methods clear to the Examiner.

Answers without working may not gain full credit.



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2. A car of mass 1000 kg is towing a caravan of mass 750 kg along a straight horizontal road. The caravan is connected to the car by a tow-bar which is parallel to the direction of motion of the car and the caravan. The tow-bar is modelled as a light rod. The engine of the car provides a constant driving force of 3200 N. The resistances to the motion of the car and the caravan are modelled as constant forces of magnitude 800 newtons and R newtons respectively.

Given that the acceleration of the car and the caravan is 0.88 ms^{-2} ,

- (a) show that $R=860$, **(3)**

- (b) find the tension in the tow-bar. **(3)**



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3. Three forces \mathbf{F}_1 , \mathbf{F}_2 and \mathbf{F}_3 acting on a particle P are given by

$$\mathbf{F}_1 = (7\mathbf{i} - 9\mathbf{j}) \text{ N}$$

$$\mathbf{F}_2 = (5\mathbf{i} + 6\mathbf{j}) \text{ N}$$

$$\mathbf{F}_3 = (p\mathbf{i} + q\mathbf{j}) \text{ N}$$

where p and q are constants.

Given that P is in equilibrium,

(a) find the value of p and the value of q . **(3)**

The force \mathbf{F}_3 is now removed. The resultant of \mathbf{F}_1 and \mathbf{F}_2 is \mathbf{R} .
Find

(b) the magnitude of \mathbf{R} , **(2)**

(c) the angle, to the nearest degree, that the direction of \mathbf{R} makes with \mathbf{j} . **(3)**



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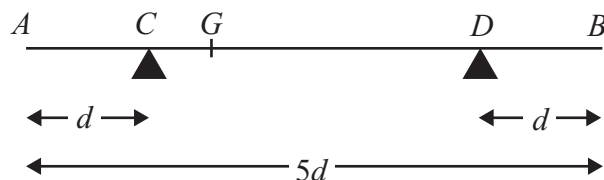


Figure 1

A non-uniform rod AB , of mass m and length $5d$, rests horizontally in equilibrium on two supports at C and D , where $AC = DB = d$, as shown in Figure 1. The centre of mass of the rod is at the point G . A particle of mass $\frac{5}{2}m$ is placed on the rod at B and the rod is on the point of tipping about D .

(a) Show that $GD = \frac{5}{2}d$. (4)

The particle is moved from B to the mid-point of the rod and the rod remains in equilibrium.

(b) Find the magnitude of the normal reaction between the support at D and the rod. (5)



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Question 4 continued

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5. A stone is projected vertically upwards from a point A with speed $u \text{ m s}^{-1}$. After projection the stone moves freely under gravity until it returns to A . The time between the instant that the stone is projected and the instant that it returns to A is $3\frac{4}{7}$ seconds.

Modelling the stone as a particle,

(a) show that $u = 17\frac{1}{2}$, **(3)**

(b) find the greatest height above A reached by the stone, **(2)**

(c) find the length of time for which the stone is at least $6\frac{3}{5}$ m above A . **(6)**



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7. [In this question, the unit vectors \mathbf{i} and \mathbf{j} are due east and due north respectively. Position vectors are relative to a fixed origin O .]

A boat P is moving with constant velocity $(-4\mathbf{i} + 8\mathbf{j})$ km h⁻¹.

(a) Calculate the speed of P . (2)

When $t = 0$, the boat P has position vector $(2\mathbf{i} - 8\mathbf{j})$ km. At time t hours, the position vector of P is \mathbf{p} km.

(b) Write down \mathbf{p} in terms of t . (1)

A second boat Q is also moving with constant velocity. At time t hours, the position vector of Q is \mathbf{q} km, where

$$\mathbf{q} = 18\mathbf{i} + 12\mathbf{j} - t(6\mathbf{i} + 8\mathbf{j})$$

Find

(c) the value of t when P is due west of Q , (3)

(d) the distance between P and Q when P is due west of Q . (3)



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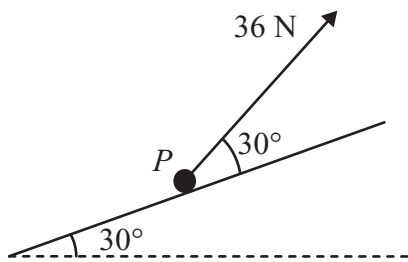


Figure 2

A particle P of mass 4 kg is moving up a fixed rough plane at a constant speed of 16 m s^{-1} under the action of a force of magnitude 36 N . The plane is inclined at 30° to the horizontal. The force acts in the vertical plane containing the line of greatest slope of the plane through P , and acts at 30° to the inclined plane, as shown in Figure 2. The coefficient of friction between P and the plane is μ . Find

- (a) the magnitude of the normal reaction between P and the plane, (4)
- (b) the value of μ . (5)

The force of magnitude 36 N is removed.

- (c) Find the distance that P travels between the instant when the force is removed and the instant when it comes to rest. (5)



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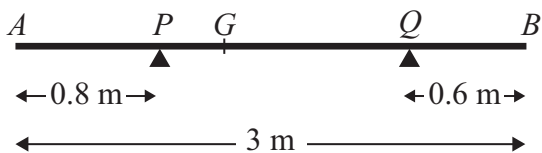


Figure 1

A non-uniform rod AB has length 3 m and mass 4.5 kg. The rod rests in equilibrium, in a horizontal position, on two smooth supports at P and at Q , where $AP = 0.8$ m and $QB = 0.6$ m, as shown in Figure 1. The centre of mass of the rod is at G . Given that the magnitude of the reaction of the support at P on the rod is twice the magnitude of the reaction of the support at Q on the rod, find

(a) the magnitude of the reaction of the support at Q on the rod, (3)

(b) the distance AG . (4)



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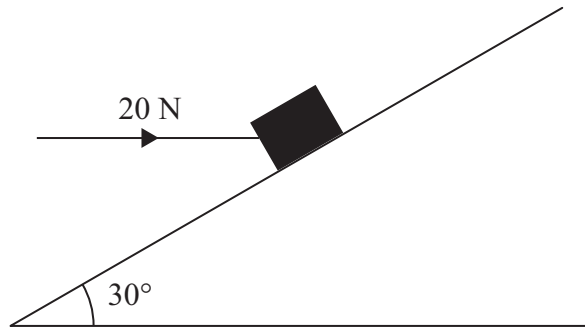


Figure 2

A box of mass 5 kg lies on a rough plane inclined at 30° to the horizontal. The box is held in equilibrium by a horizontal force of magnitude 20 N, as shown in Figure 2. The force acts in a vertical plane containing a line of greatest slope of the inclined plane. The box is in equilibrium and on the point of moving down the plane. The box is modelled as a particle.

Find

(a) the magnitude of the normal reaction of the plane on the box, (4)

(b) the coefficient of friction between the box and the plane. (5)

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4. A car is moving on a straight horizontal road. At time $t = 0$, the car is moving with speed 20 m s^{-1} and is at the point A . The car maintains the speed of 20 m s^{-1} for 25 s. The car then moves with constant deceleration 0.4 m s^{-2} , reducing its speed from 20 m s^{-1} to 8 m s^{-1} . The car then moves with constant speed 8 m s^{-1} for 60 s. The car then moves with constant acceleration until it is moving with speed 20 m s^{-1} at the point B .

(a) Sketch a speed-time graph to represent the motion of the car from A to B .

(3)

(b) Find the time for which the car is decelerating.

(2)

Given that the distance from A to B is 1960 m,

(c) find the time taken for the car to move from A to B .

(8)



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5. A particle P is projected vertically upwards from a point A with speed $u \text{ m s}^{-1}$. The point A is 17.5 m above horizontal ground. The particle P moves freely under gravity until it reaches the ground with speed 28 m s^{-1} .

(a) Show that $u = 21$ (3)

At time t seconds after projection, P is 19 m above A .

(b) Find the possible values of t . (5)

The ground is soft and, after P reaches the ground, P sinks vertically downwards into the ground before coming to rest. The mass of P is 4 kg and the ground is assumed to exert a constant resistive force of magnitude 5000 N on P .

(c) Find the vertical distance that P sinks into the ground before coming to rest. (4)



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6. [In this question \mathbf{i} and \mathbf{j} are horizontal unit vectors due east and due north respectively and position vectors are given with respect to a fixed origin.]

A ship S is moving with constant velocity $(-12\mathbf{i} + 7.5\mathbf{j}) \text{ km h}^{-1}$.

(a) Find the direction in which S is moving, giving your answer as a bearing. (3)

At time t hours after noon, the position vector of S is \mathbf{s} km. When $t = 0$, $\mathbf{s} = 40\mathbf{i} - 6\mathbf{j}$.

(b) Write down \mathbf{s} in terms of t . (2)

A fixed beacon B is at the point with position vector $(7\mathbf{i} + 12.5\mathbf{j}) \text{ km}$.

(c) Find the distance of S from B when $t = 3$ (4)

(d) Find the distance of S from B when S is due north of B . (4)



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Question 6 continued

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Figure 3

Two particles P and Q , of mass 0.3 kg and 0.5 kg respectively, are joined by a light horizontal rod. The system of the particles and the rod is at rest on a horizontal plane. At time $t = 0$, a constant force F of magnitude 4 N is applied to Q in the direction PQ , as shown in Figure 3. The system moves under the action of this force until $t = 6$ s. During the motion, the resistance to the motion of P has constant magnitude 1 N and the resistance to the motion of Q has constant magnitude 2 N.

Find

- (a) the acceleration of the particles as the system moves under the action of F , (3)
- (b) the speed of the particles at $t = 6$ s, (2)
- (c) the tension in the rod as the system moves under the action of F . (3)

At $t = 6$ s, F is removed and the system decelerates to rest. The resistances to motion are unchanged. Find

- (d) the distance moved by P as the system decelerates, (4)
- (e) the thrust in the rod as the system decelerates. (3)



Centre No.							Paper Reference				Surname	Initial(s)	
Candidate No.					6	6	7	7	/	0	1	Signature	

Paper Reference(s)

6677/01

Edexcel GCE

Mechanics M1

Advanced/Advanced Subsidiary

Wednesday 23 January 2013 – Morning

Time: 1 hour 30 minutes

Examiner’s use only

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Team Leader’s use only

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Question Number	Leave Blank
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Materials required for examination **Items included with question papers**
 Mathematical Formulae (Pink) Nil

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation or symbolic differentiation/integration, or have retrievable mathematical formulae stored in them.

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature. Check that you have the correct question paper.
 Answer ALL the questions.
 You must write your answer to each question in the space following the question.
 Whenever a numerical value of g is required, take $g = 9.8 \text{ m s}^{-2}$.
 When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information for Candidates

A booklet ‘Mathematical Formulae and Statistical Tables’ is provided.
 Full marks may be obtained for answers to ALL questions.
 The marks for individual questions and the parts of questions are shown in round brackets: e.g. (2).
 There are 7 questions in this question paper. The total mark for this paper is 75.
 There are 28 pages in this question paper. Any blank pages are indicated.

Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled.
 You should show sufficient working to make your methods clear to the Examiner.
 Answers without working may not gain full credit.

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2. A steel girder AB , of mass 200 kg and length 12 m, rests horizontally in equilibrium on two smooth supports at C and at D , where $AC = 2$ m and $DB = 2$ m. A man of mass 80 kg stands on the girder at the point P , where $AP = 4$ m, as shown in Figure 1.

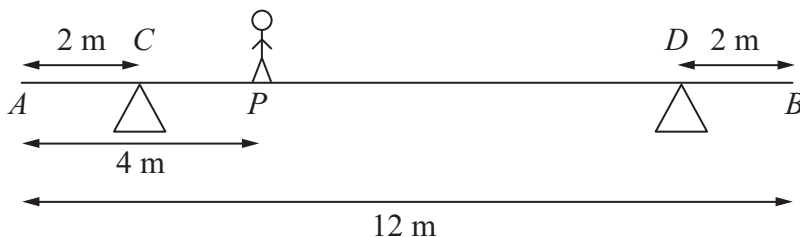


Figure 1

The man is modelled as a particle and the girder is modelled as a uniform rod.

- (a) Find the magnitude of the reaction on the girder at the support at C . (3)

The support at D is now moved to the point X on the girder, where $XB = x$ metres. The man remains on the girder at P , as shown in Figure 2.

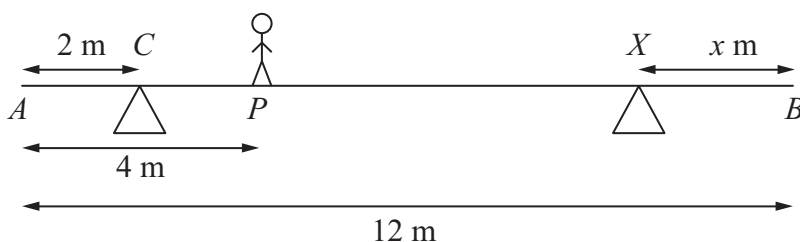


Figure 2

Given that the magnitudes of the reactions at the two supports are now equal and that the girder again rests horizontally in equilibrium, find

- (b) the magnitude of the reaction at the support at X , (2)
 (c) the value of x . (4)



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3. A particle P of mass 2 kg is attached to one end of a light string, the other end of which is attached to a fixed point O . The particle is held in equilibrium, with OP at 30° to the downward vertical, by a force of magnitude F newtons. The force acts in the same vertical plane as the string and acts at an angle of 30° to the horizontal, as shown in Figure 3.

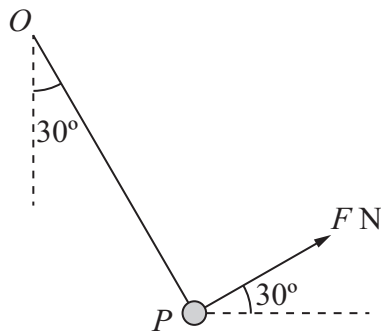


Figure 3

Find

- (i) the value of F ,
- (ii) the tension in the string.

(8)



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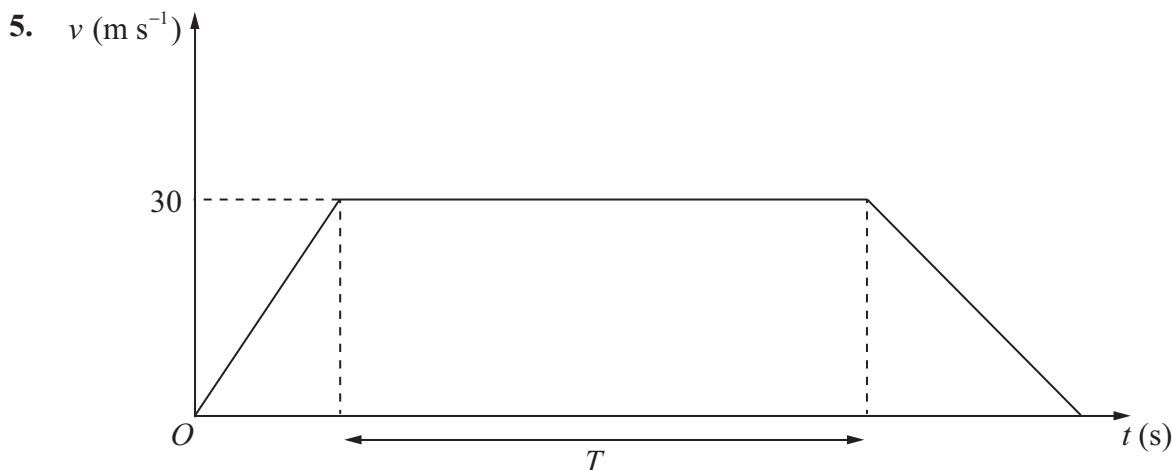


Figure 4

The velocity-time graph in Figure 4 represents the journey of a train *P* travelling along a straight horizontal track between two stations which are 1.5 km apart. The train *P* leaves the first station, accelerating uniformly from rest for 300 m until it reaches a speed of 30 m s^{-1} . The train then maintains this speed for T seconds before decelerating uniformly at 1.25 m s^{-2} , coming to rest at the next station.

(a) Find the acceleration of *P* during the first 300 m of its journey. (2)

(b) Find the value of T . (5)

A second train *Q* completes the same journey in the same total time. The train leaves the first station, accelerating uniformly from rest until it reaches a speed of $V \text{ m s}^{-1}$ and then immediately decelerates uniformly until it comes to rest at the next station.

(c) Sketch on the diagram above, a velocity-time graph which represents the journey of train *Q*. (2)

(d) Find the value of V . (6)



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Question 6 continued

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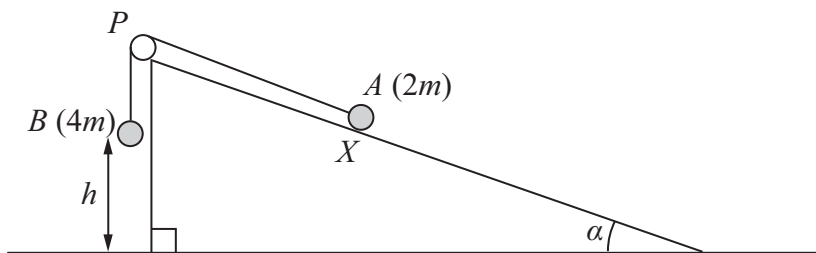


Figure 5

Figure 5 shows two particles A and B , of mass $2m$ and $4m$ respectively, connected by a light inextensible string. Initially A is held at rest on a rough inclined plane which is fixed to horizontal ground. The plane is inclined to the horizontal at an angle α , where $\tan \alpha = \frac{3}{4}$. The coefficient of friction between A and the plane is $\frac{1}{4}$. The string passes over a small smooth pulley P which is fixed at the top of the plane. The part of the string from A to P is parallel to a line of greatest slope of the plane and B hangs vertically below P . The system is released from rest with the string taut, with A at the point X and with B at a height h above the ground.

For the motion until B hits the ground,

- (a) give a reason why the magnitudes of the accelerations of the two particles are the same, (1)
- (b) write down an equation of motion for each particle, (4)
- (c) find the acceleration of each particle. (5)

Particle B does not rebound when it hits the ground and A continues moving up the plane towards P . Given that A comes to rest at the point Y , without reaching P ,

- (d) find the distance XY in terms of h . (6)



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1. Two particles A and B , of mass 2 kg and 3 kg respectively, are moving towards each other in opposite directions along the same straight line on a smooth horizontal surface. The particles collide directly. Immediately before the collision the speed of A is 5 m s^{-1} and the speed of B is 6 m s^{-1} . The magnitude of the impulse exerted on B by A is 14 N s . Find

(a) the speed of A immediately after the collision, **(3)**

(b) the speed of B immediately after the collision. **(3)**



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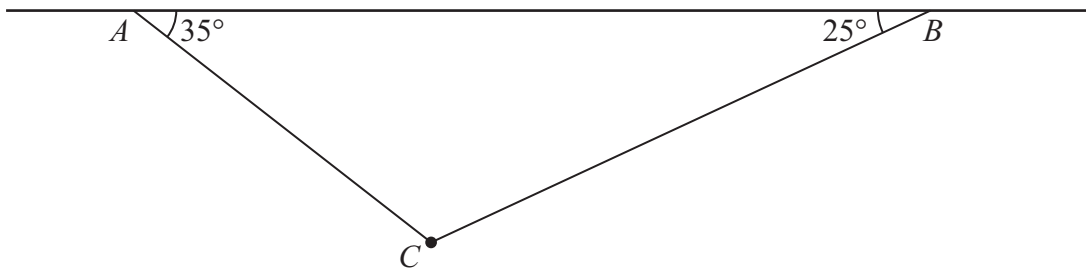


Figure 1

A particle of weight 8 N is attached at C to the ends of two light inextensible strings AC and BC. The other ends, A and B, are attached to a fixed horizontal ceiling. The particle hangs at rest in equilibrium, with the strings in a vertical plane. The string AC is inclined at 35° to the horizontal and the string BC is inclined at 25° to the horizontal, as shown in Figure 1. Find

- (i) the tension in the string AC,
- (ii) the tension in the string BC.

(8)



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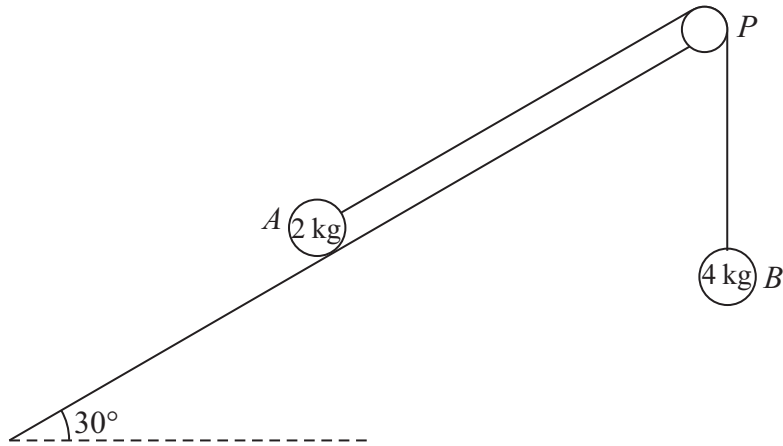


Figure 2

A fixed rough plane is inclined at 30° to the horizontal. A small smooth pulley P is fixed at the top of the plane. Two particles A and B , of mass 2 kg and 4 kg respectively, are attached to the ends of a light inextensible string which passes over the pulley P . The part of the string from A to P is parallel to a line of greatest slope of the plane and B hangs freely below P , as shown in Figure 2. The coefficient of friction between A and the plane is $\frac{1}{\sqrt{3}}$. Initially A is held at rest on the plane. The particles are released from rest with the string taut and A moves up the plane.

Find the tension in the string immediately after the particles are released.

(9)



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4. At time $t = 0$, two balls A and B are projected vertically upwards. The ball A is projected vertically upwards with speed 2 m s^{-1} from a point 50 m above the horizontal ground. The ball B is projected vertically upwards from the ground with speed 20 m s^{-1} . At time $t = T$ seconds, the two balls are at the same vertical height, h metres, above the ground. The balls are modelled as particles moving freely under gravity. Find

(a) the value of T ,

(5)

(b) the value of h .

(2)



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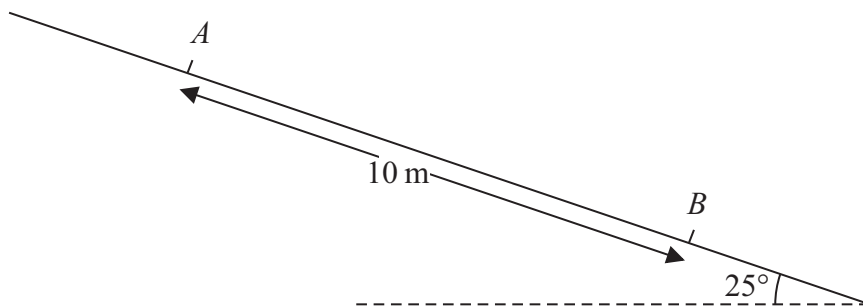


Figure 3

A particle P of mass 0.6 kg slides with constant acceleration down a line of greatest slope of a rough plane, which is inclined at 25° to the horizontal. The particle passes through two points A and B , where $AB = 10$ m, as shown in Figure 3. The speed of P at A is 2 m s⁻¹. The particle P takes 3.5 s to move from A to B . Find

- (a) the speed of P at B , (3)
- (b) the acceleration of P , (2)
- (c) the coefficient of friction between P and the plane. (5)



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6. [In this question \mathbf{i} and \mathbf{j} are horizontal unit vectors due east and due north respectively. Position vectors are given with respect to a fixed origin O .]

A ship S is moving with constant velocity $(3\mathbf{i} + 3\mathbf{j}) \text{ km h}^{-1}$. At time $t = 0$, the position vector of S is $(-4\mathbf{i} + 2\mathbf{j}) \text{ km}$.

(a) Find the position vector of S at time t hours. (2)

A ship T is moving with constant velocity $(-2\mathbf{i} + n\mathbf{j}) \text{ km h}^{-1}$. At time $t = 0$, the position vector of T is $(6\mathbf{i} + \mathbf{j}) \text{ km}$. The two ships meet at the point P .

(b) Find the value of n . (5)

(c) Find the distance OP . (4)



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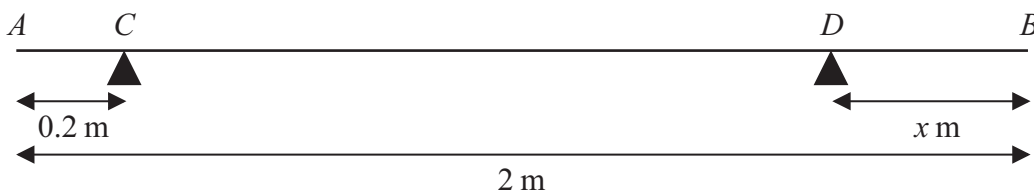


Figure 5

A uniform rod AB has length 2 m and mass 50 kg. The rod is in equilibrium in a horizontal position, resting on two smooth supports at C and D , where $AC = 0.2$ metres and $DB = x$ metres, as shown in Figure 5. Given that the magnitude of the reaction on the rod at D is twice the magnitude of the reaction on the rod at C ,

(a) find the value of x .

(6)

The support at D is now moved to the point E on the rod, where $EB = 0.4$ metres. A particle of mass m kg is placed on the rod at B , and the rod remains in equilibrium in a horizontal position. Given that the magnitude of the reaction on the rod at E is four times the magnitude of the reaction on the rod at C ,

(b) find the value of m .

(7)



1. Particle P has mass 3 kg and particle Q has mass $m \text{ kg}$. The particles are moving in opposite directions along a smooth horizontal plane when they collide directly. Immediately before the collision, the speed of P is 4 m s^{-1} and the speed of Q is 3 m s^{-1} . In the collision the direction of motion of P is unchanged and the direction of motion of Q is reversed. Immediately after the collision, the speed of P is 1 m s^{-1} and the speed of Q is 1.5 m s^{-1} .

(a) Find the magnitude of the impulse exerted on P in the collision.

(3)

(b) Find the value of m .

(3)



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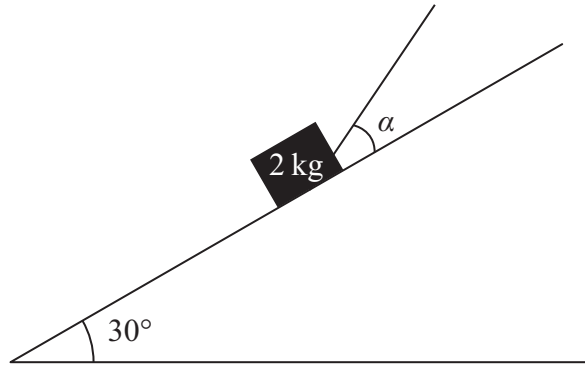


Figure 1

A box of mass 2 kg is held in equilibrium on a fixed rough inclined plane by a rope. The rope lies in a vertical plane containing a line of greatest slope of the inclined plane. The rope is inclined to the plane at an angle α , where $\tan \alpha = \frac{3}{4}$, and the plane is at an angle of 30° to the horizontal, as shown in Figure 1. The coefficient of friction between the box and the inclined plane is $\frac{1}{3}$ and the box is on the point of slipping up the plane. By modelling the box as a particle and the rope as a light inextensible string, find the tension in the rope.

(8)



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Question 3 continued

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5. A car is travelling along a straight horizontal road. The car takes 120 s to travel between two sets of traffic lights which are 2145 m apart. The car starts from rest at the first set of traffic lights and moves with constant acceleration for 30 s until its speed is 22 m s^{-1} . The car maintains this speed for T seconds. The car then moves with constant deceleration, coming to rest at the second set of traffic lights.

(a) Sketch, in the space below, a speed-time graph for the motion of the car between the two sets of traffic lights.

(2)

(b) Find the value of T .

(3)

A motorcycle leaves the first set of traffic lights 10 s after the car has left the first set of traffic lights. The motorcycle moves from rest with constant acceleration, $a \text{ m s}^{-2}$, and passes the car at the point A which is 990 m from the first set of traffic lights. When the motorcycle passes the car, the car is moving with speed 22 m s^{-1} .

(c) Find the time it takes for the motorcycle to move from the first set of traffic lights to the point A .

(4)

(d) Find the value of a .

(2)



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Question 6 continued

Lined writing area containing horizontal lines for the answer to Question 6.



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7. [In this question, the horizontal unit vectors \mathbf{i} and \mathbf{j} are directed due east and due north respectively.]

The velocity, \mathbf{v} m s⁻¹, of a particle P at time t seconds is given by

$$\mathbf{v} = (1 - 2t)\mathbf{i} + (3t - 3)\mathbf{j}$$

- (a) Find the speed of P when $t = 0$ **(3)**

- (b) Find the bearing on which P is moving when $t = 2$ **(2)**

- (c) Find the value of t when P is moving
 - (i) parallel to \mathbf{j} ,
 - (ii) parallel to $(-\mathbf{i} - 3\mathbf{j})$.**(6)**



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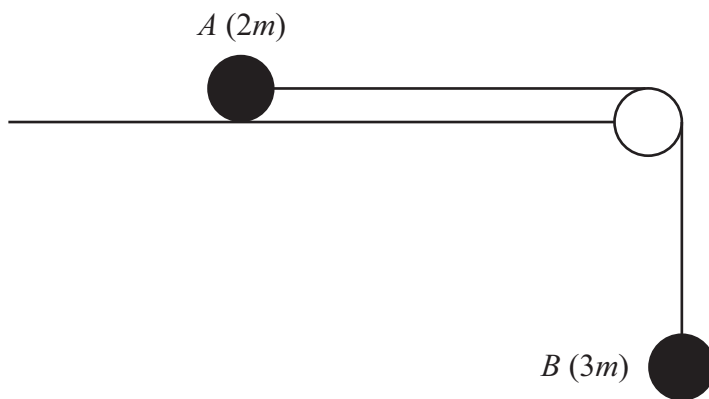


Figure 2

Two particles A and B have masses $2m$ and $3m$ respectively. The particles are attached to the ends of a light inextensible string. Particle A is held at rest on a smooth horizontal table. The string passes over a small smooth pulley which is fixed at the edge of the table. Particle B hangs at rest vertically below the pulley with the string taut, as shown in Figure 2. Particle A is released from rest. Assuming that A has not reached the pulley, find

- (a) the acceleration of B , (5)
- (b) the tension in the string, (1)
- (c) the magnitude and direction of the force exerted on the pulley by the string. (4)



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Question 8 continued

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Q8

(Total 10 marks)

TOTAL FOR PAPER: 75 MARKS

END

